
Coalescent Likelihood Methods

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Outline

1. **Introduction to coalescent theory**
2. Practical example
3. Genealogy samplers
4. Break
5. Survey of samplers
6. Evolutionary forces
7. Practical considerations

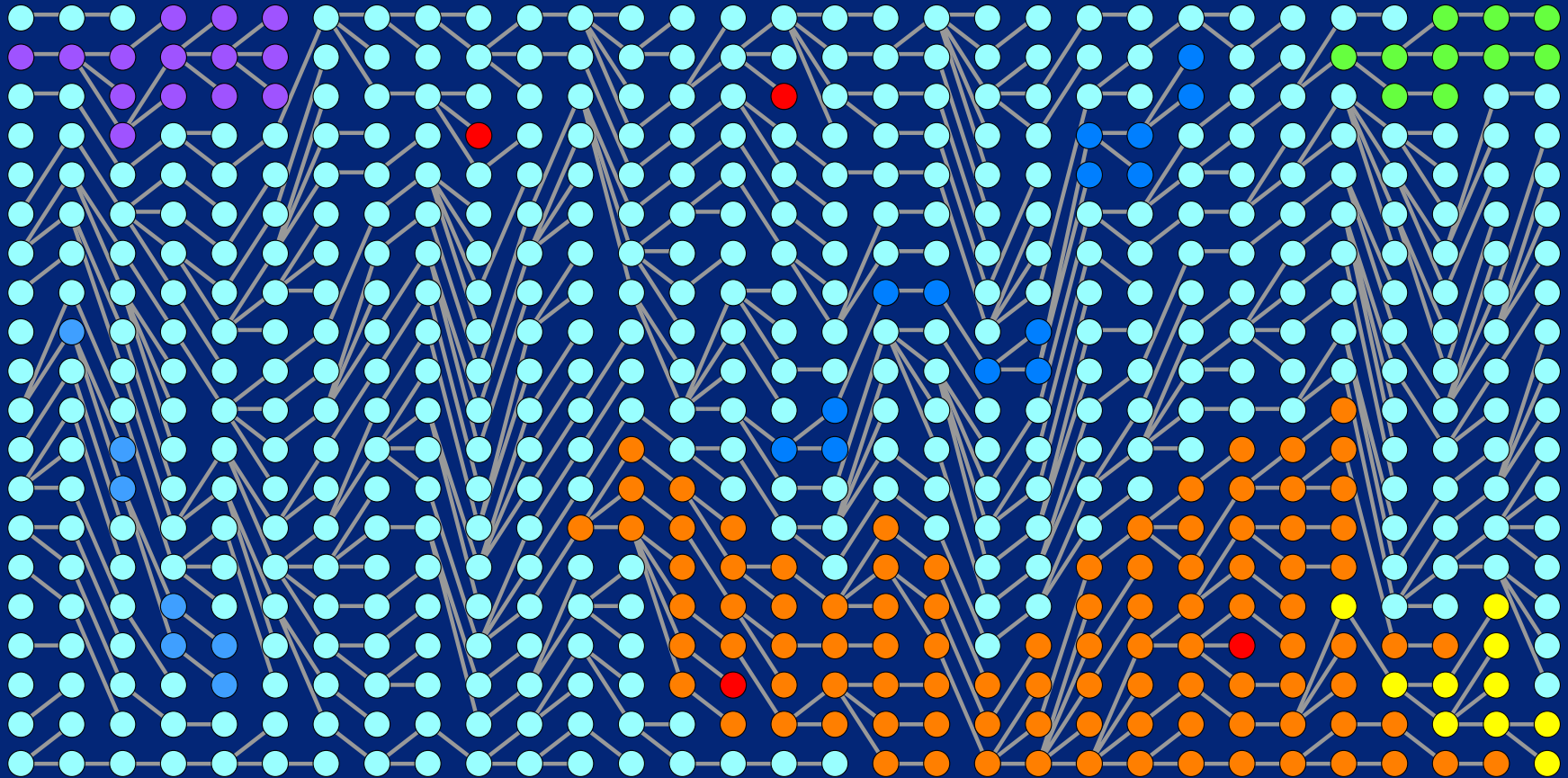
Population genetics can help us to find answers

- We are interested in questions like
 - How big is this population?
 - Are these populations isolated? How common is migration?
 - How fast have they been growing or shrinking?
 - What is the recombination rate across this region?
 - Is this locus under selection?
- All of these questions require comparison of many individuals.

Coalescent-based studies

- How many gray whales were there prior to whaling?
- When was the common ancestor of HIV lines in a Libyan hospital?
- Is the highland/lowland distinction in Andean ducks recent or ancient?
- Did humans wipe out the Beringian bison population?
- What proportion of HIV virions in a patient actually contribute to the breeding pool?
- What is the direction of gene flow between European rabbit populations?

Basics: Wright-Fisher population model



All individuals release many gametes and new individuals for the next generation are formed randomly from these.

Wright-Fisher population model

- Population size N is constant through time.
- Each individual gets replaced every generation.
- Next generation is drawn randomly from a large gamete pool.
- Only genetic drift affects the allele frequencies.

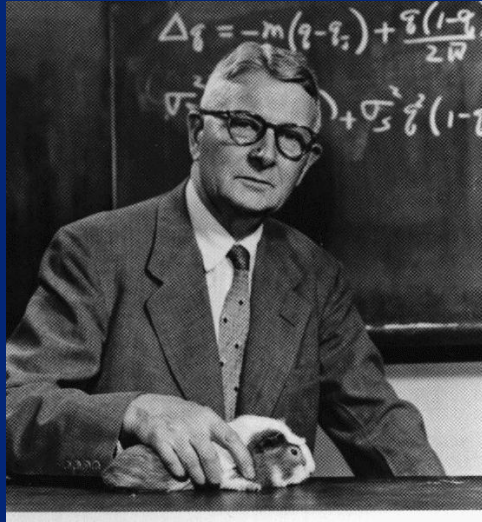
Other population models

- Other population models can often be equated to Wright-Fisher
- The N parameter becomes the effective population size N_e
- For example, cyclic populations have an N_e that is the harmonic mean of the various sizes

The big trick

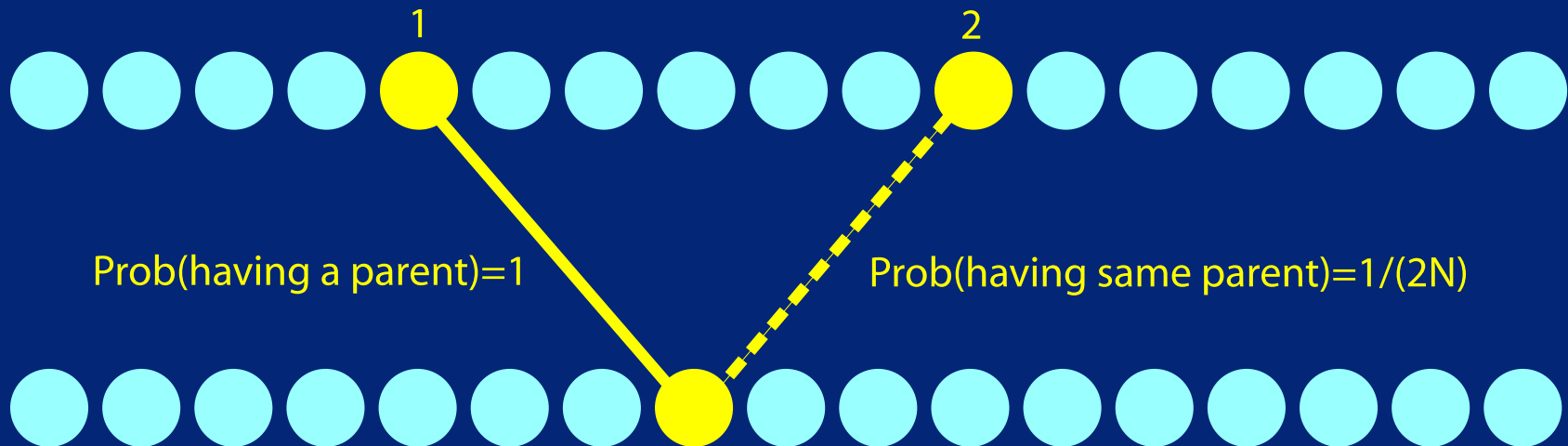
- We have a model for the progress of a population forward in time
- What we observe is the end product: genetic data today
- We want to reverse this model so that it tells us about the *past* of our sequences

The Coalescent

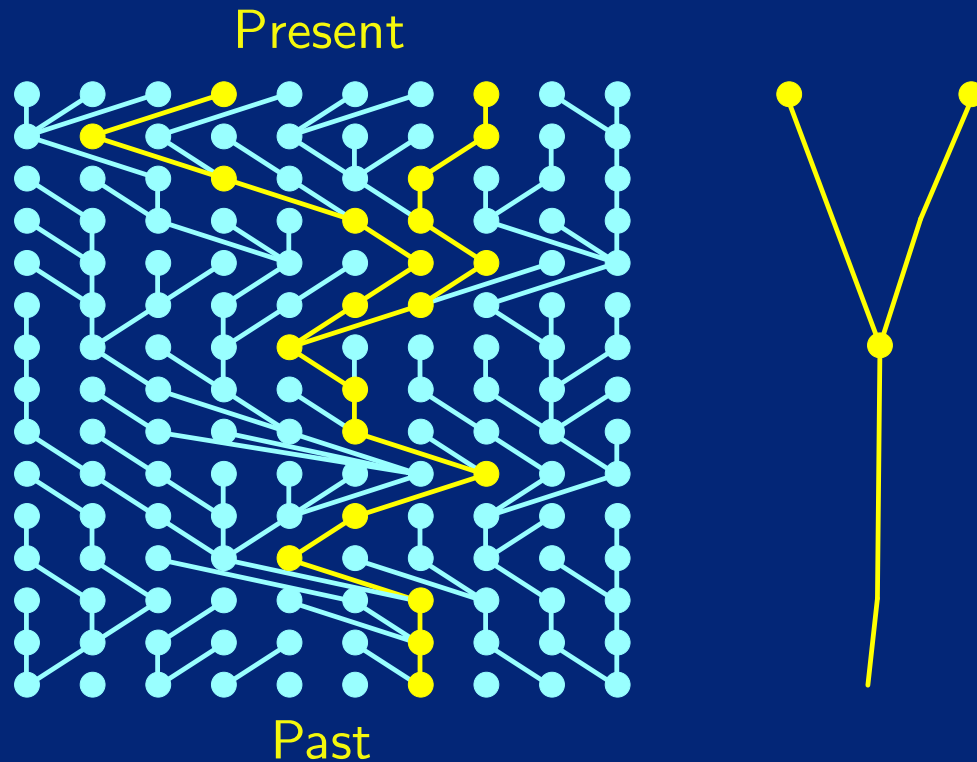


Sewall Wright showed that the probability that 2 gene copies come from the same gene copy in the preceding generation is

$$\text{Prob (two genes share a parent)} = \frac{1}{2N}$$



The Coalescent



In every generation, there is a chance of $1/2N$ to coalesce. Following the sampled lineages through generations backwards in time we realize that it follows a geometric distribution with

$$\mathbb{E}(u) = 2N \quad [\text{the expectation of the time of coalescence } u \text{ of **two** tips is } 2N]$$

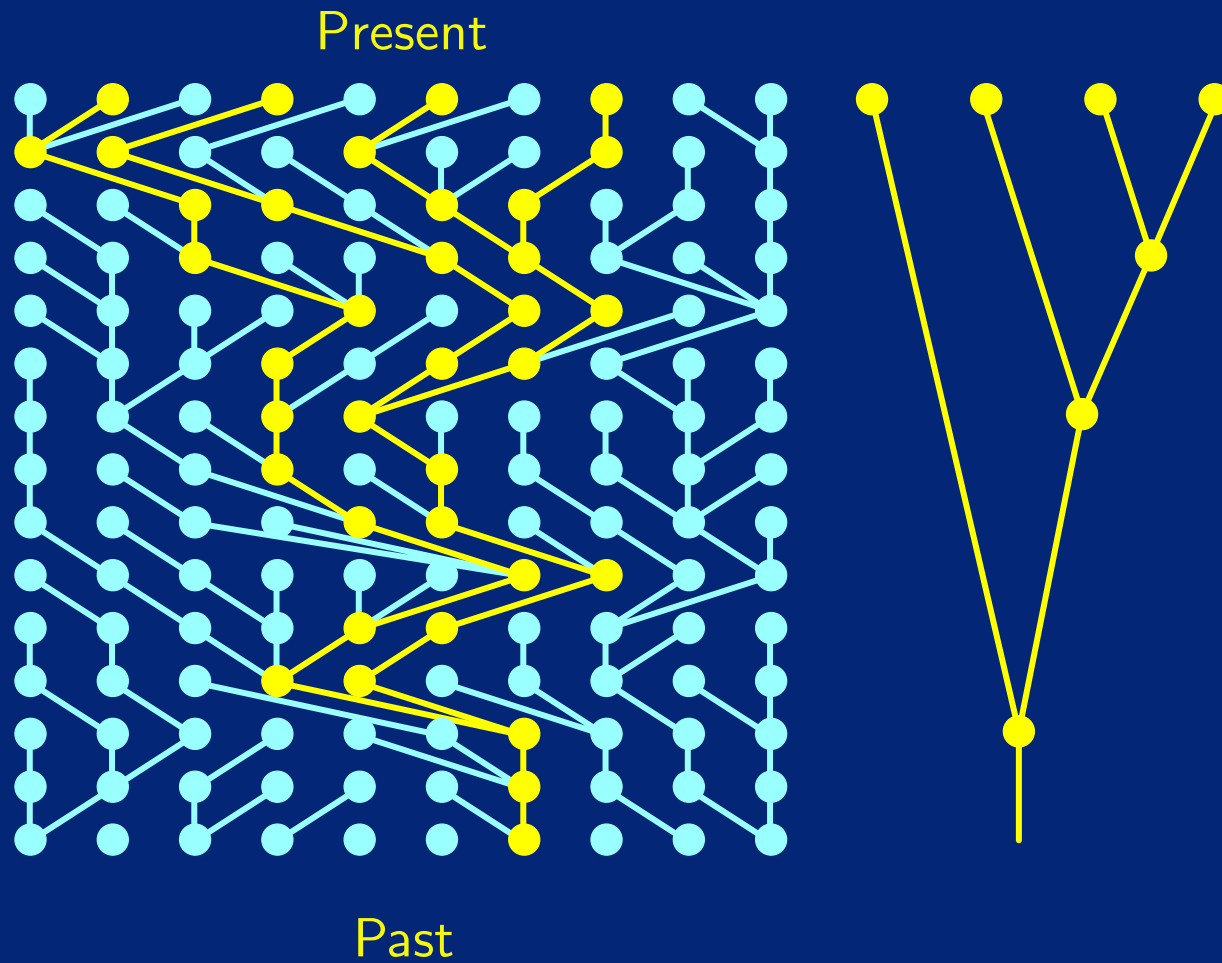
The Coalescent



JFC Kingman generalized this for k gene copies.

$$\text{Prob } (k \text{ copies are reduced to } k - 1 \text{ copies}) = \frac{k(k - 1)}{4N}$$

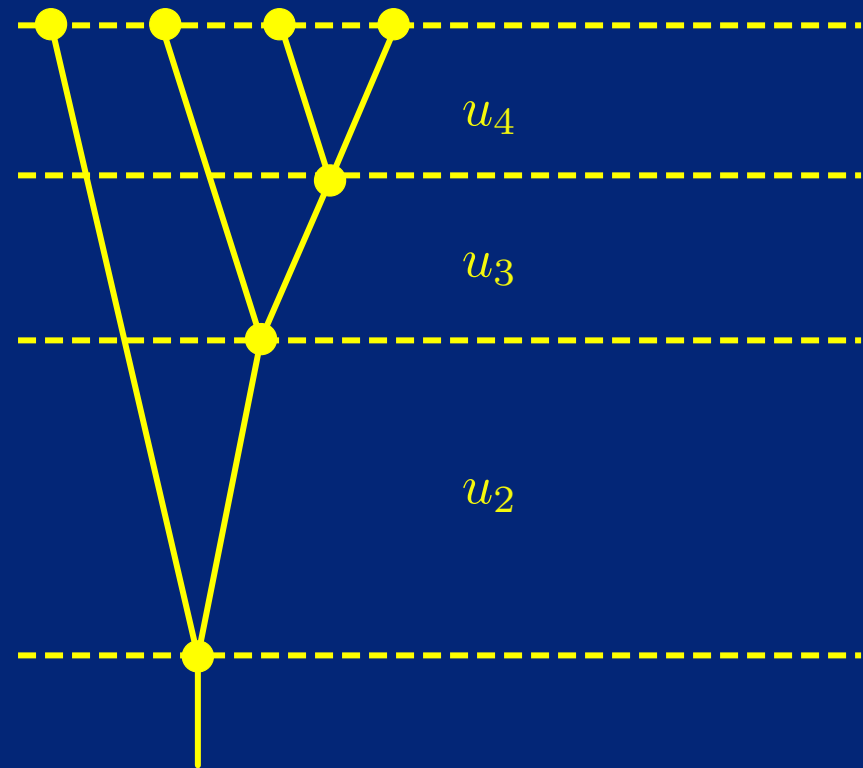
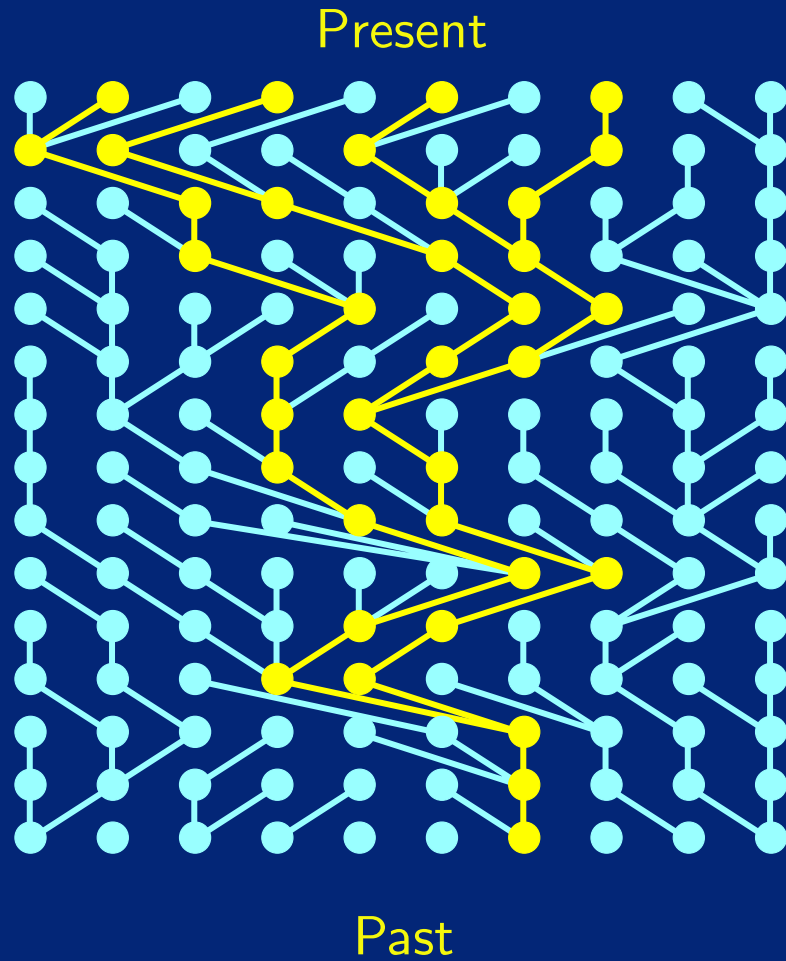
Kingman's n -coalescent



Kingman's n -coalescent

The expectation for the time interval u_k is

$$\mathbb{E}(u_k) = \frac{4N}{k(k-1)}$$



$$p(G|N) = \prod_i \exp\left(-u_i \frac{k(k-1)}{4N}\right) \frac{1}{2N}$$

The Θ parameter

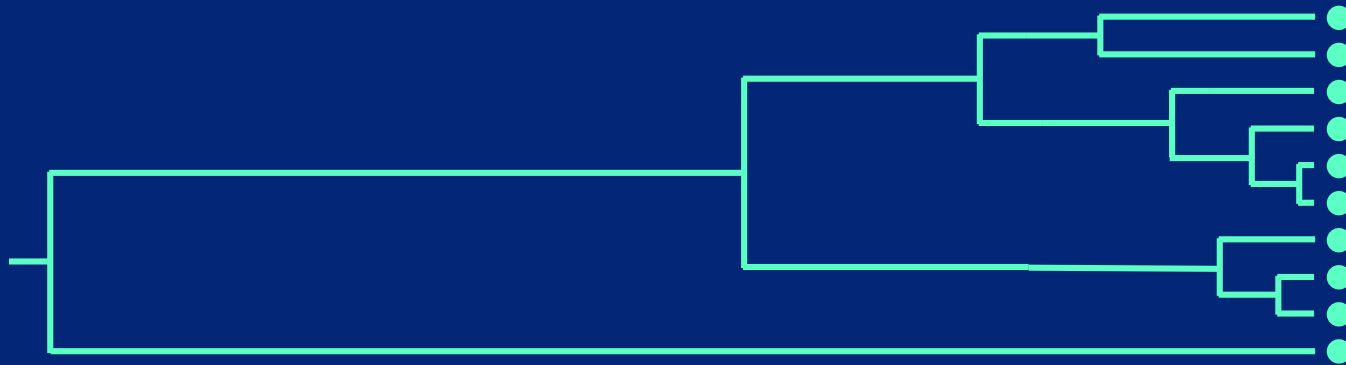
- The n-coalescent is defined in terms of N_e and time.
- We cannot measure time just by looking at genes, though we can measure divergence.
- We rescale the equations in terms of N_e , time, and the mutation rate μ .
- We can no longer estimate N_e but only the composite parameter Θ .
- $\Theta = 4N_e\mu$ in diploids.
- Multiple time point data can separate N_e and μ

What is this coalescent thing good for?



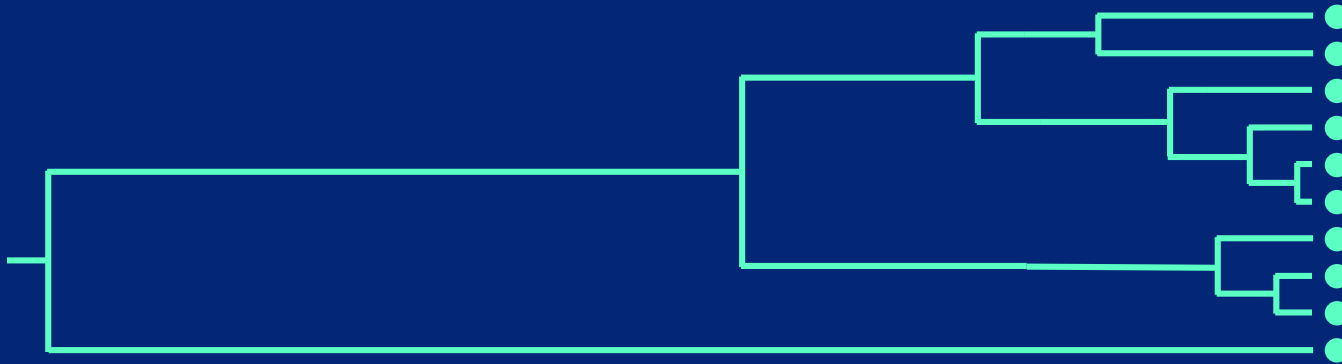
Utopian population size estimator

1. We get the correct genealogy from an infallible oracle
2. We know that we can calculate $p(\text{Genealogy}|\mathbb{N})$



Utopian population size estimator

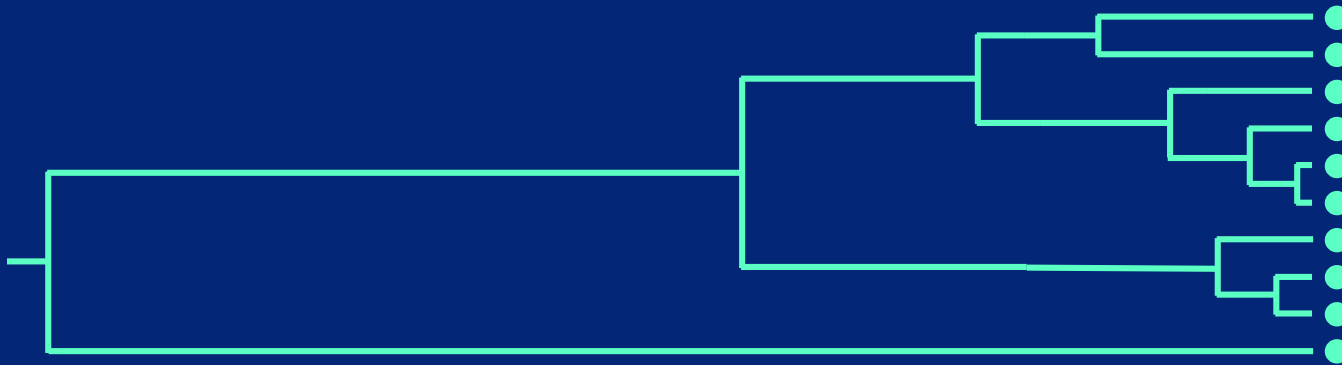
1. We get the correct genealogy from an infallible oracle
2. We remember the probability calculation



$$p(G|N) = p(u_1|N, k) \frac{1}{2N} \times p(u_2|N, k - 1) \frac{1}{2N} \times \dots$$

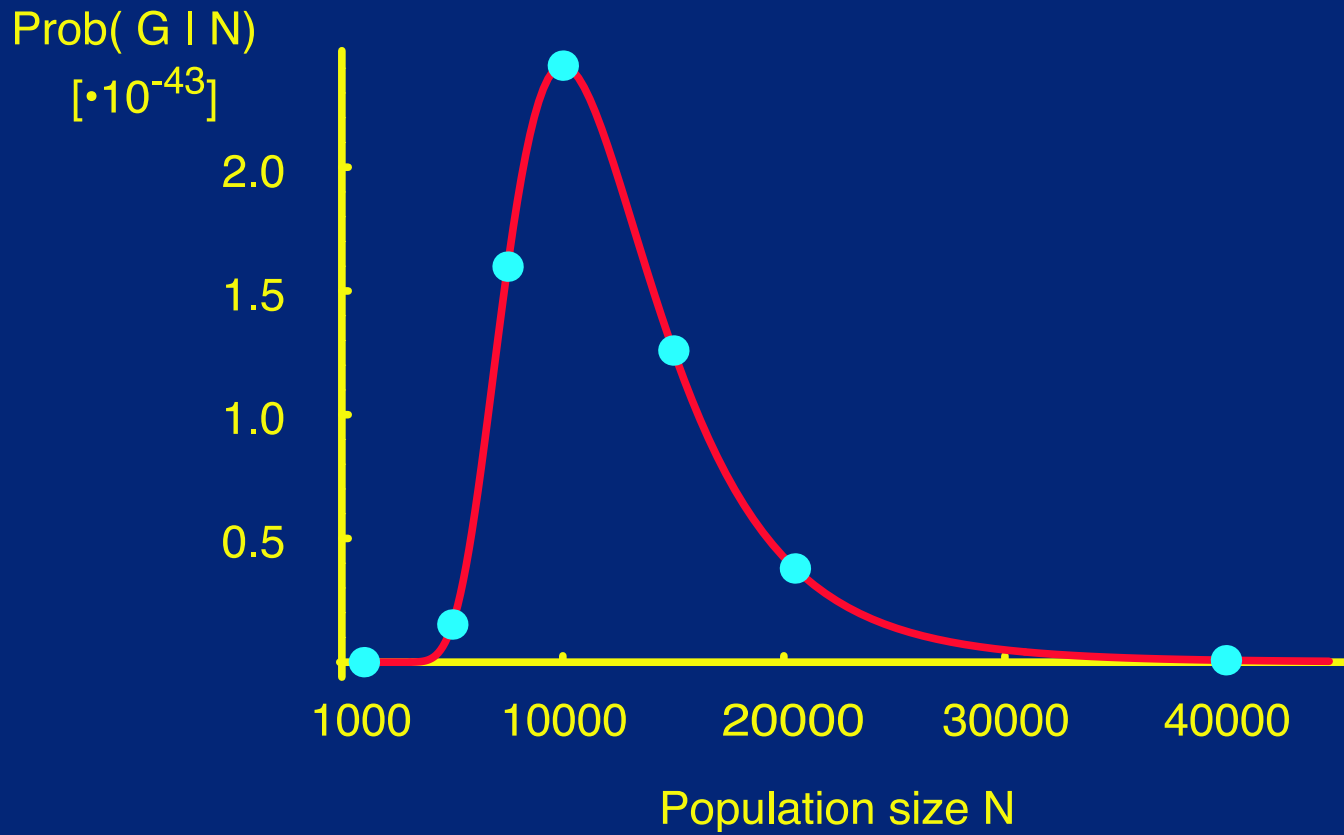
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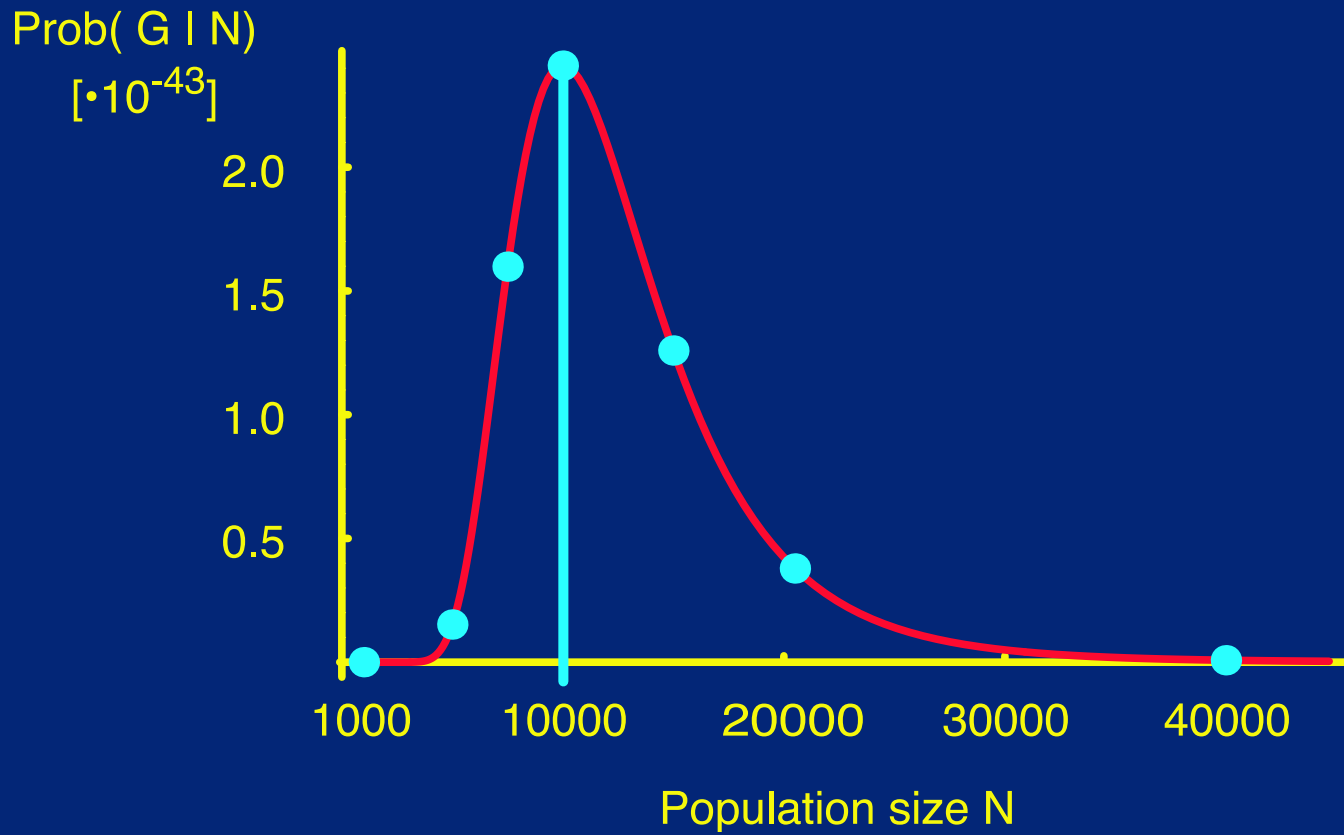


$$p(\text{Genealogy}|\mathbf{N}) = \prod_j^T e^{-u_j \frac{k_j(k_j-1)}{4N}} \frac{1}{2N}$$

Utopian population size estimator

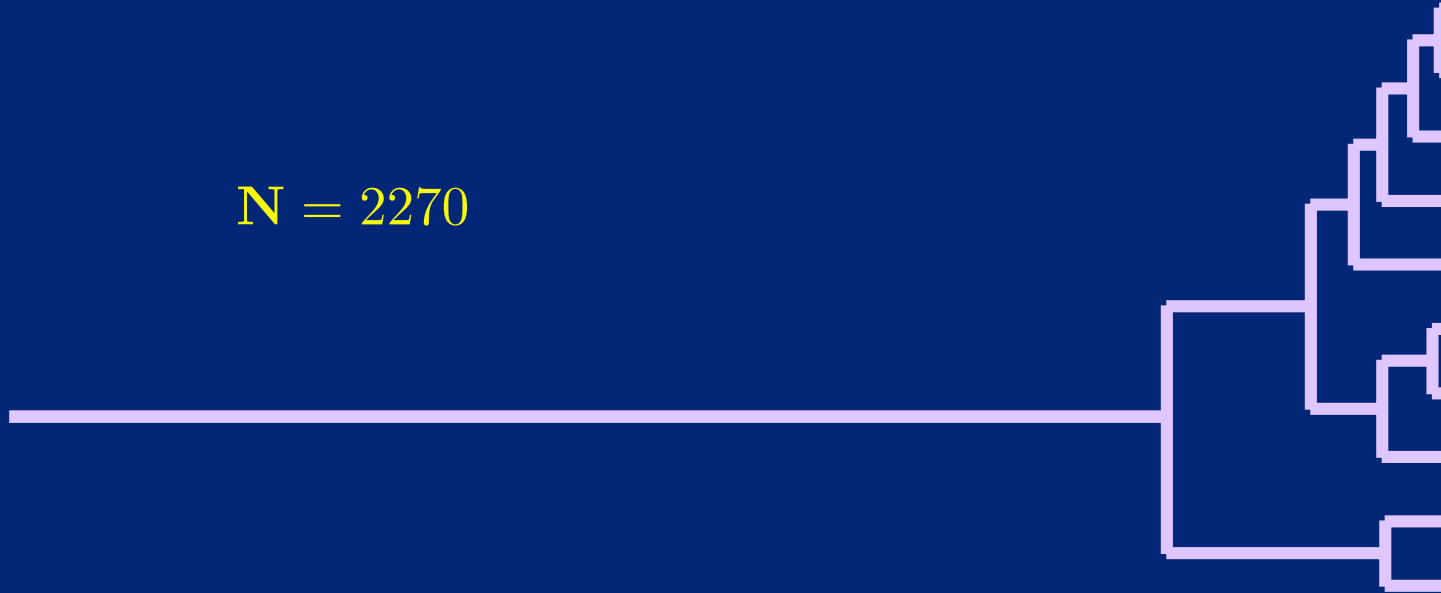


Utopian population size estimator

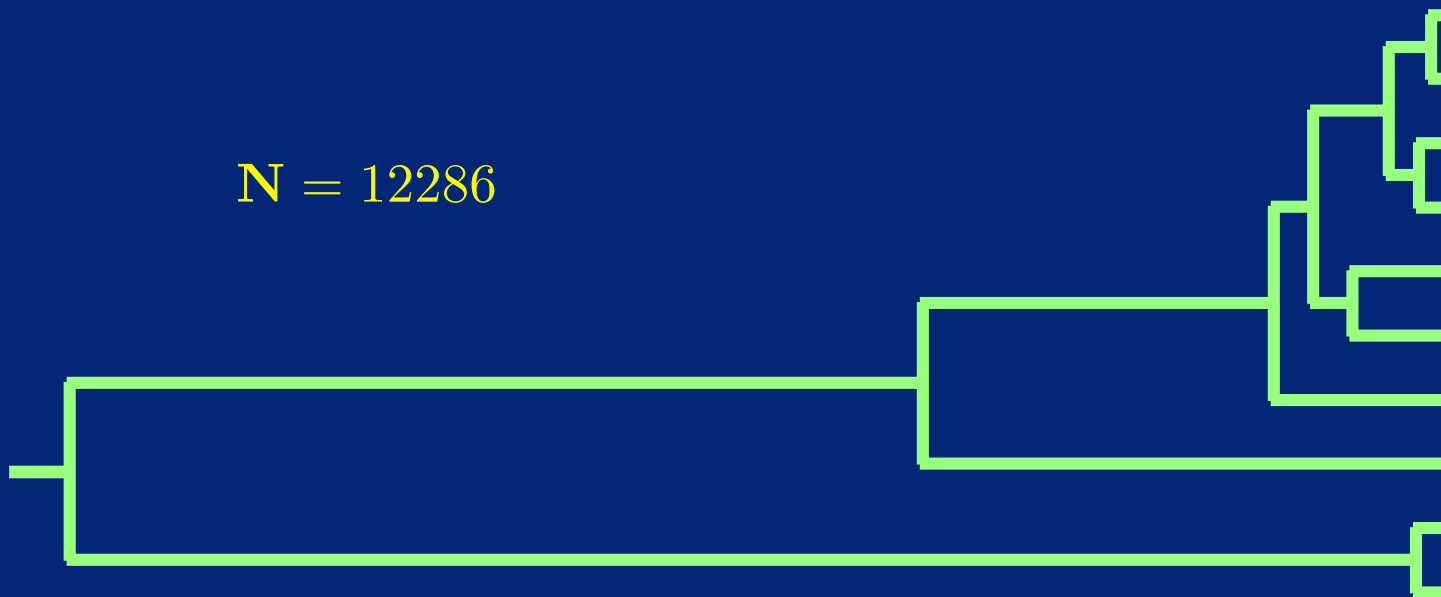


Utopian population size estimator

$N = 2270$



$N = 12286$



Lack of infallible oracles

- We assume we know the true genealogy including branch lengths
- We don't really know that
- We probably can't even infer it:
 - Tree inference is hard in general
 - Population data usually don't have enough information for good tree inference

Non-likelihood use of coalescent

- Summary statistics
 - Watterson's estimator of θ
 - F_{ST} (estimates θ and/or migration rate)
 - Hudson's and Wakeley's estimators of recombination rate
- Known-tree methods
 - UPBLUE (Yang)
 - Skyline plots (Strimmer, Pybus, Rambaut)

These methods are conceptually easy, but not always powerful, and they are difficult to extend to complex cases.

Genealogy samplers

- Acknowledge that there is an underlying genealogy–
 - but we don't know it
 - we can't infer it with high certainty
 - we can't sum over all possibilities
- A directed sample of plausible genealogies–
 - can capture much of the information in the unknown true genealogy
 - takes a long time but not forever
- These are **genealogy sampler** methods

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1. Introduction to coalescent theory
2. **Practical example: red drum**
3. Genealogy samplers
4. Break
5. Survey of samplers
6. Evolutionary forces
7. Practical considerations

What is the effective population size of red drum?

Red drum, *Sciaenops ocellatus*, are large fish found in the Gulf of Mexico.



Turner, Wares, and Gold

Genetic effective size is three orders of magnitude smaller than adult census size in an abundant, estuarine-dependent marine fish

Genetics 162:1329-1339 (2002)

What is the effective population size of red drum?

- Census population size: 3,400,000
- Effective population size: ?
- Data set:
 - 8 microsatellite loci
 - 7 populations
 - 20 individuals per population

What is the effective population size of red drum?

Three approaches:

1. Allele frequency fluctuation from year to year

- Measures current population size
- May be sensitive to short-term fluctuations

2. Coalescent estimate from *Migrate*

- Measures long-term harmonic mean of population size
- May reflect past bottlenecks or other long-term effects

3. Demographic models

- Attempt to infer genetic size from census size
- Vulnerable to errors in demographic model
- Not well established for long-lived species with high reproductive variability

Population model used for Migrate

- Multiple populations along Gulf coast
- Migration allowed only between adjacent populations
- Allowing for population structure should improve estimates of population size



What is the effective population size of red drum?

Estimates:

Census size (N):	3,400,000
Allele frequency method (N_e):	3,516 (1,785-18,148)
Coalescent method (N_e):	1,853 (317-7,226)

The demographic model can be made consistent with these only by assuming enormous variance in reproductive success among individuals.

What is the effective population size of red drum?

- Allele frequency estimators measure current size
- Coalescent estimators measure long-term size
- Conclusion: population size and structure have been stable

What is the effective population size of red drum?

- Effective population size at least 1000 times smaller than census
- This result was highly surprising
- Red drum has the genetic liabilities of a rare species
- Turner et al. hypothesize an “estuary lottery”
- Unless the eggs are in exactly the right place, they all die

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Coalescent estimation of population parameters

- Mutation model: Steal a likelihood model from phylogeny inference
- Population genetics model: the Coalescent

Coalescent estimation of population parameters

$$L(\Theta) = P(Data|\Theta)$$

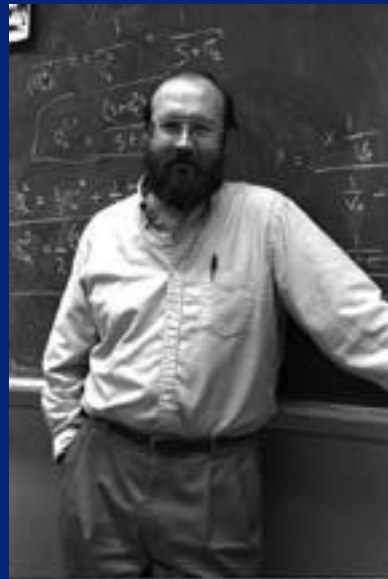
Coalescent estimation of population parameters

$$L(\Theta) = P(Data|\Theta) = \sum_G P(Data|G)P(G|\Theta)$$

Coalescent estimation of population parameters

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$P(Data|G)$ comes from a mutational model



Coalescent estimation of population parameters

$$L(\Theta) = P(Data|\Theta) = \sum_G P(Data|G)P(G|\Theta)$$

$P(G|\Theta)$ comes from the coalescent



Coalescent estimation of population parameters

$$L(\Theta) = P(Data|\Theta) = \sum_G P(Data|G)P(G|\Theta)$$

\sum_G is a problem

A solution: Markov chain Monte Carlo

- If we can't sample all genealogies, could we try a random sample?
 - Not really.
- How about a sample which focuses on good ones?
 - What is a good genealogy?
 - How can we find them in such a big search space?

A solution: Markov chain Monte Carlo



Metropolis recipe

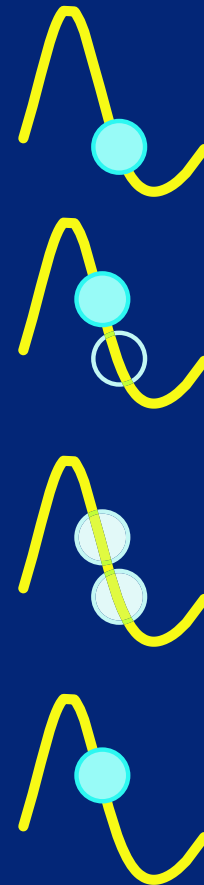
0. first state

1. perturb old state and calculate probability of new state

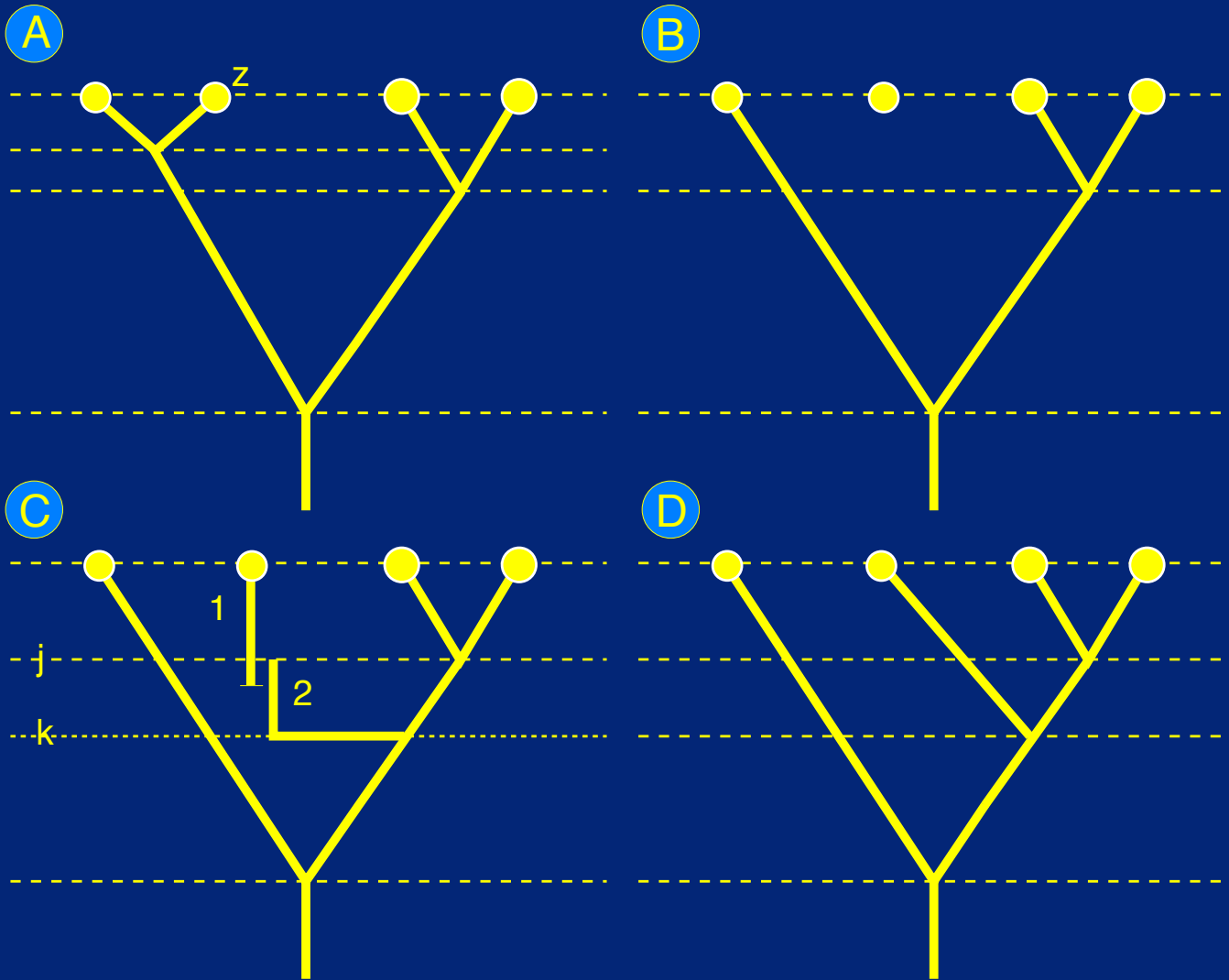
2. test if new state is better than old state: accept if ratio of new and old is larger than a random number between 0 and 1.

3. move to new state if accepted otherwise stay at old state

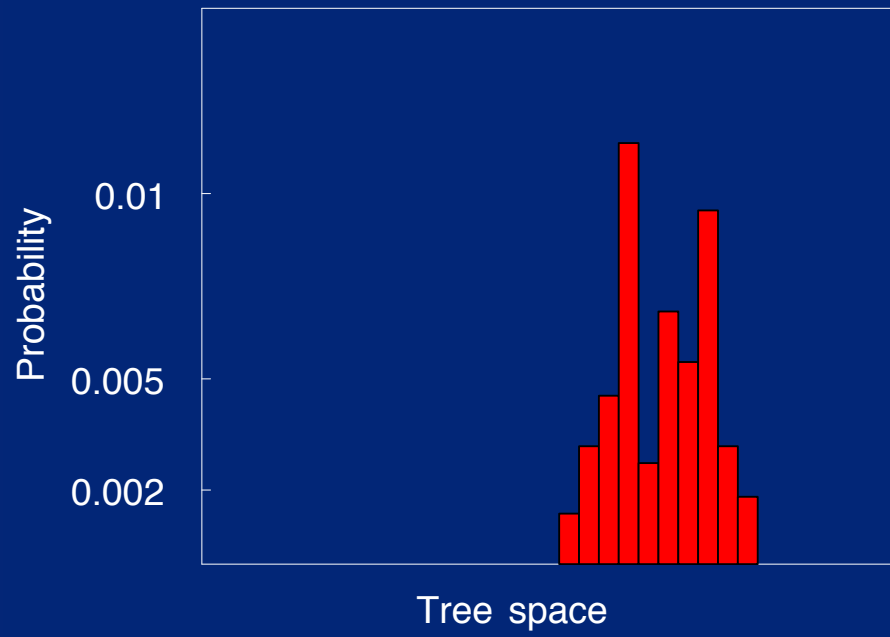
4. go to 1



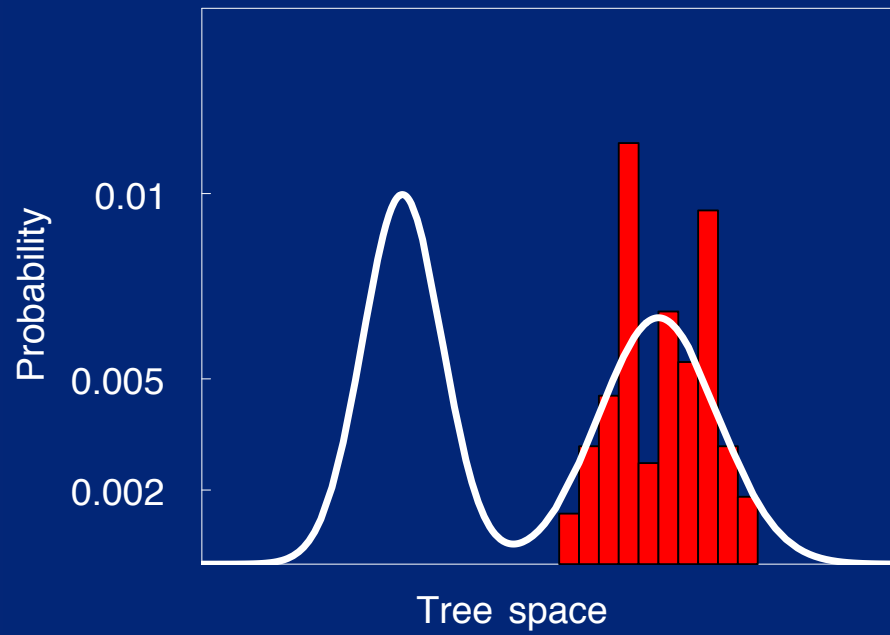
How do we change a genealogy?



MCMC walk result



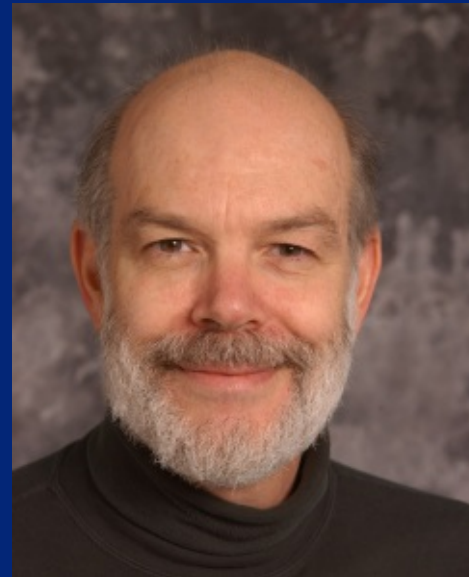
MCMC walk result—with problems



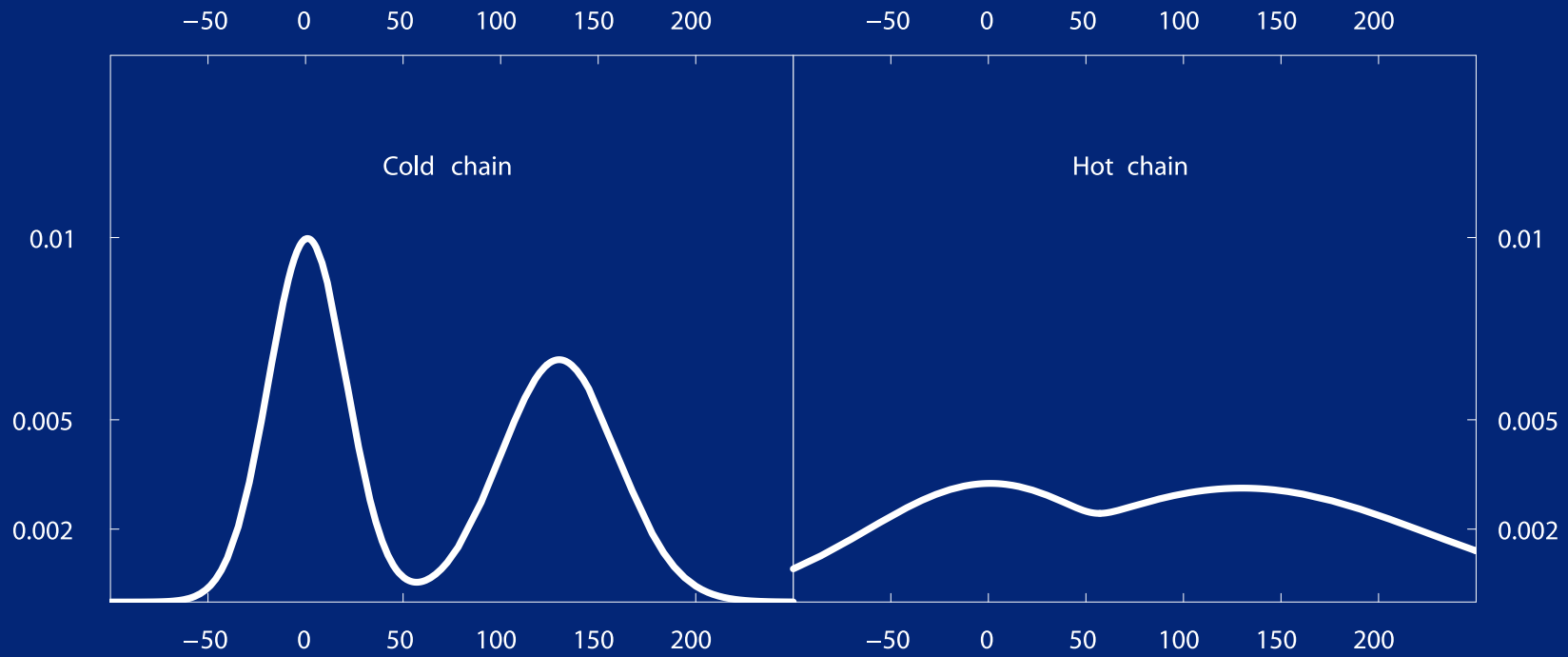
Improving our MCMC walker: Heating

Metropolis Coupled Markov chain Monte Carlo (AKA MC^3)

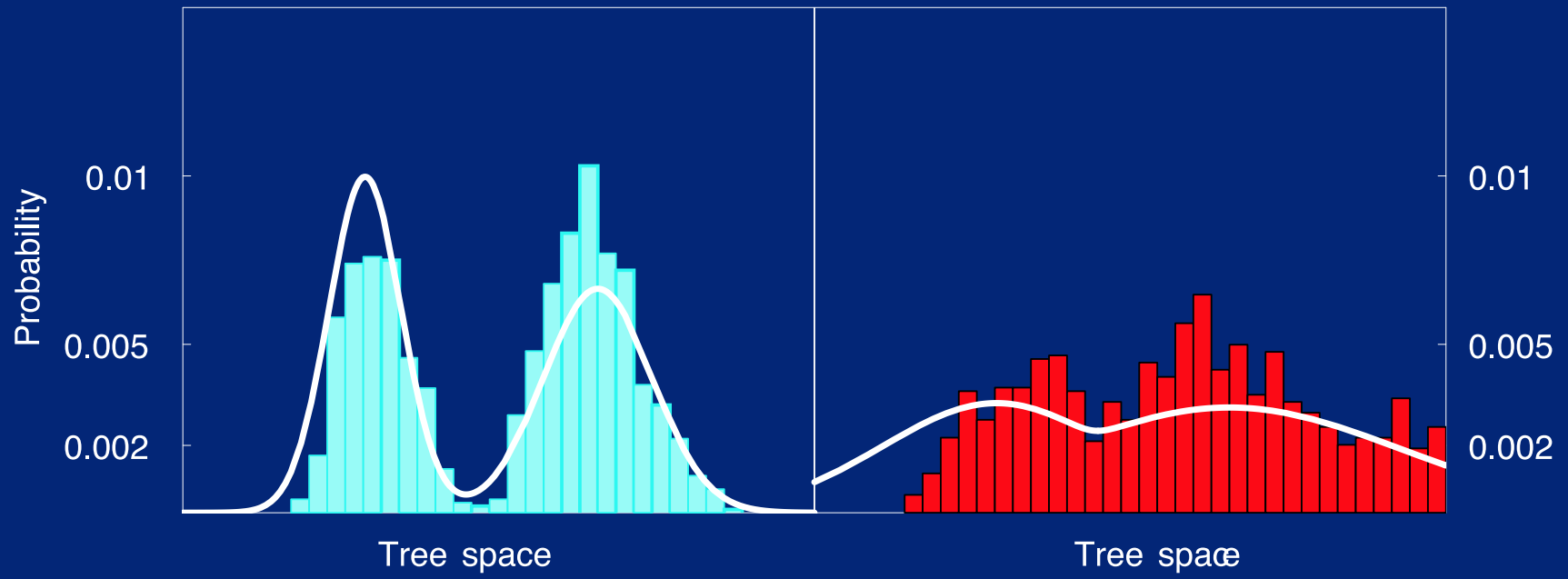
- Run several independent parallel chains: each has a different temperature
- After some sampling of genealogies, swap the genealogies of a pair of chains if the ratio between probabilities in the cold and the hot chain is larger than a random number drawn between 0 and 1.



Improving our MCMC walker: MCMCMC or MC³



better MCMC walk result



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2. Genealogy samplers
 - (a) **Likelihood version**
 - (b) **Bayesian version**
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Likelihood and Bayesian approaches

- All genealogy samplers search among genealogies
- All of them require some type of guide value (“driving value”) to determine which genealogies will be proposed
- Two major approaches: Likelihood-based and Bayesian
- Major ideological difference, relatively small practical one

Likelihood samplers

- Use arbitrary values of the parameters to guide the search
- Sample genealogies throughout the search
- At the end of the search, evaluate $P(G|\Theta)$ for sampled genealogies
- Correct for the influence of the driving values
- Iterate to improve driving values

Bayesian samplers

- Propose new driving values throughout the run
- New driving values drawn from a prior
- Accept or reject driving values based on $P(G|\Theta)$
- Final conclusions based on histogram of driving values

Likelihood analysis

We will approximate:

$$L(\Theta) = \sum_G P(Data|G)P(G|\Theta)$$

Likelihood analysis

We will approximate:

$$L(\Theta) = \sum_G P(Data|G)P(G|\Theta)$$

by sampling n genealogies from $P(Data|G)P(G|\Theta_0)$:

$$L(\Theta) = \frac{1}{n} \sum_{G^*} \frac{P(Data|G)P(G|\Theta)}{P(Data|G)P(G|\Theta_0)/L(\Theta_0)}$$

Here the G^* are no longer random genealogies; they are sampled from a distribution that depends on the **driving value** Θ_0

Likelihood analysis

$$L(\Theta) = \frac{1}{n} \sum_G \frac{P(\text{Data}|G)P(G|\Theta)}{P(\text{Data}|G)P(G|\Theta_0)/L(\Theta_0)}$$

Isn't this circular? We have a solution for the unknown $L(\Theta)$ in terms of the unknown $L(\Theta_0)$.

Likelihood analysis

$$L(\Theta) = \frac{1}{n} \sum_G \frac{P(Data|G)P(G|\Theta)}{P(Data|G)P(G|\Theta_0)/L(\Theta_0)}$$

Isn't this circular? We have a solution for the unknown $L(\Theta)$ in terms of the unknown $L(\Theta_0)$.

$$\frac{L(\Theta)}{L(\Theta_0)} = \frac{1}{n} \sum_G \frac{P(Data|G)P(G|\Theta)}{P(Data|G)P(G|\Theta_0)}$$

This doesn't give us the actual value of $L(\Theta)$ but it does allow us to compare various values of Θ and choose the best.

Likelihood analysis

- This approach is only asymptotically correct
- For finite sample sizes, it has a bias toward its driving value
- We can greatly reduce this:
 - Start with an arbitrary Θ_0
 - Run the sampler a while and estimate the best Θ
 - It will be biased toward Θ_0 , but...
 - Use it as the new Θ_0 and start over

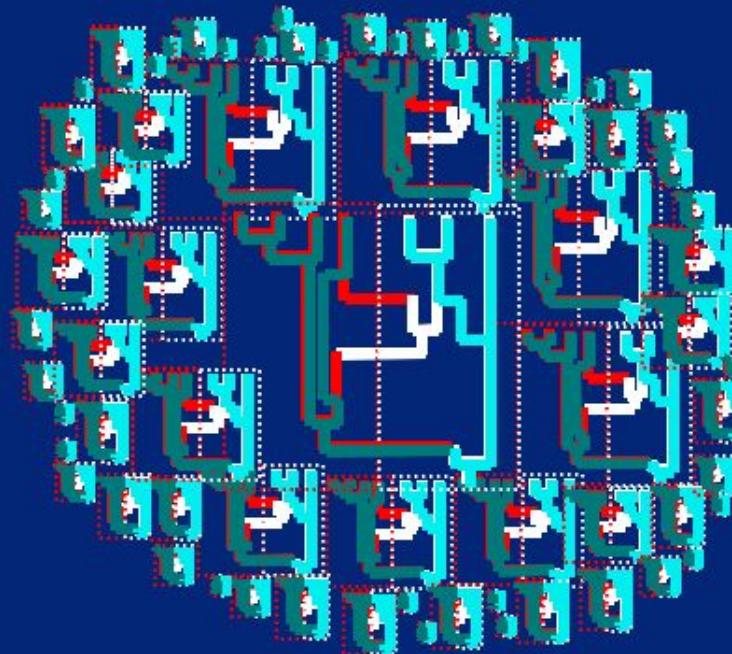
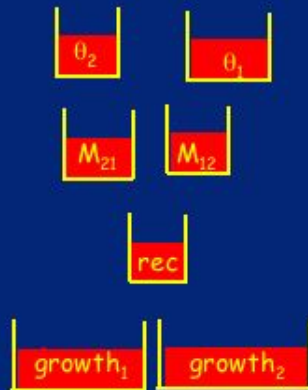
Bayesian approach

- A Bayesian analysis requires us to provide priors for all parameters
- These *could* be based on detailed knowledge of the biology
- In practice, uninformative flat priors are used

New search scheme for Bayes

Parameter space
(determined by priors)

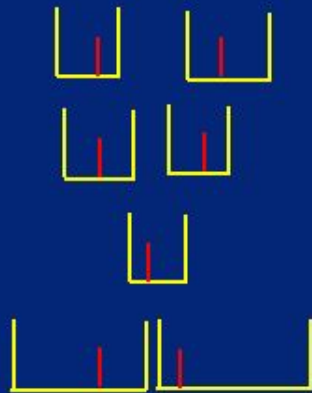
Tree space



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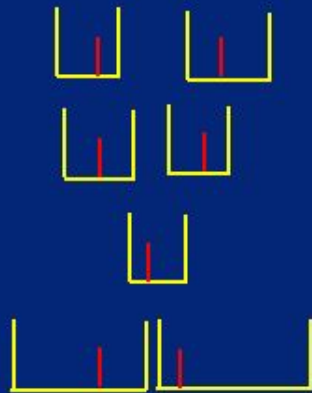
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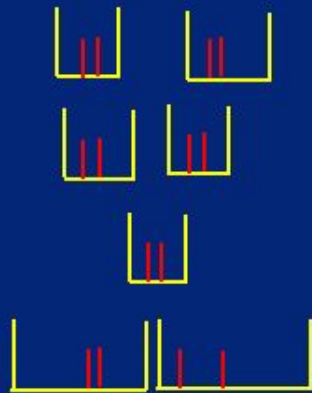
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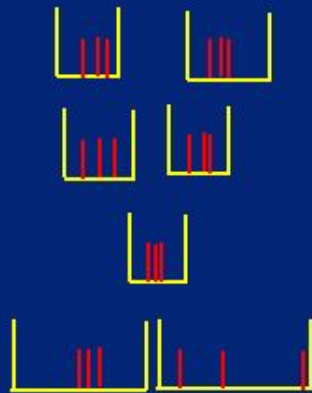
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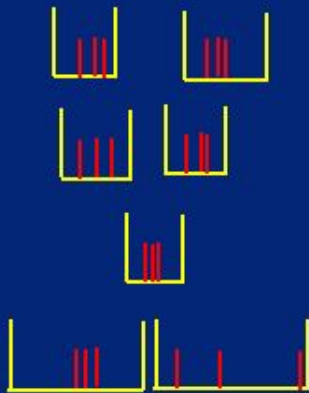
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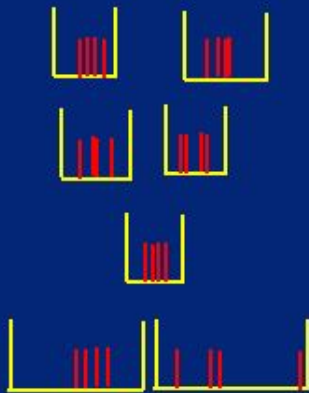
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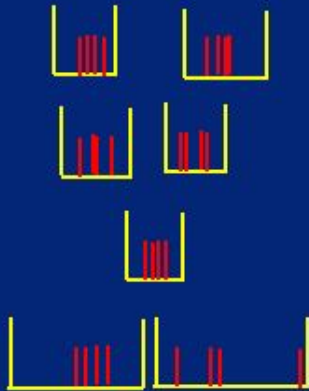
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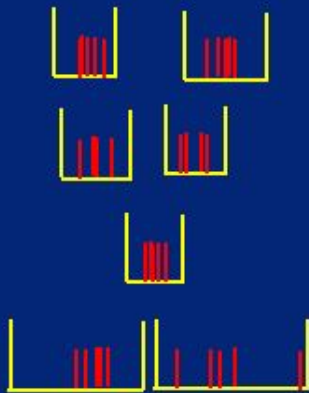
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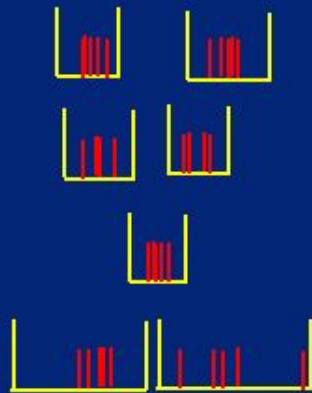
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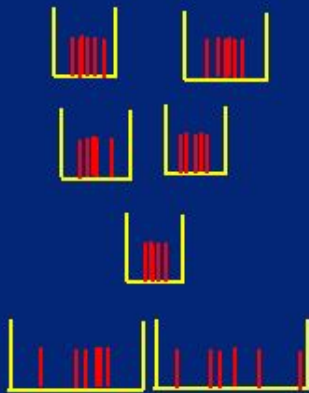
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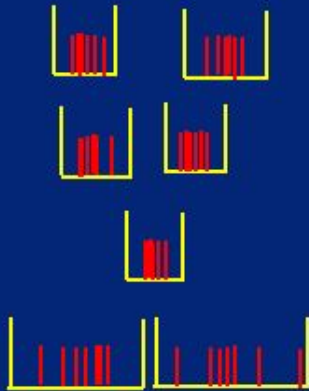
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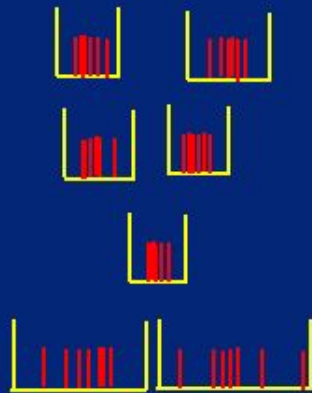
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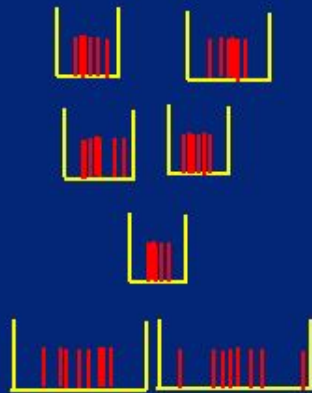


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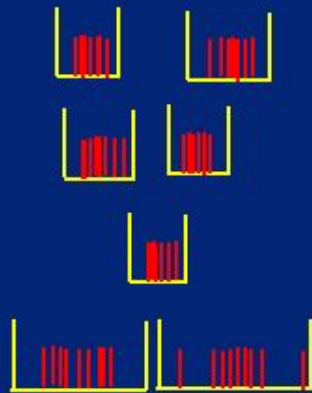


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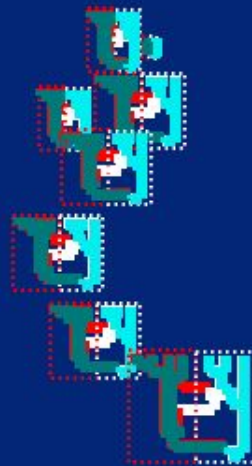


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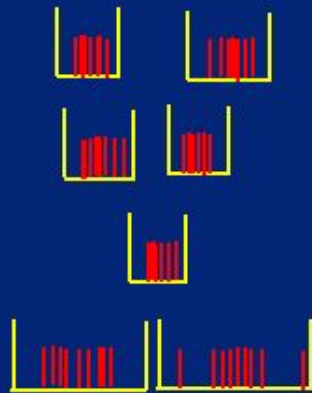


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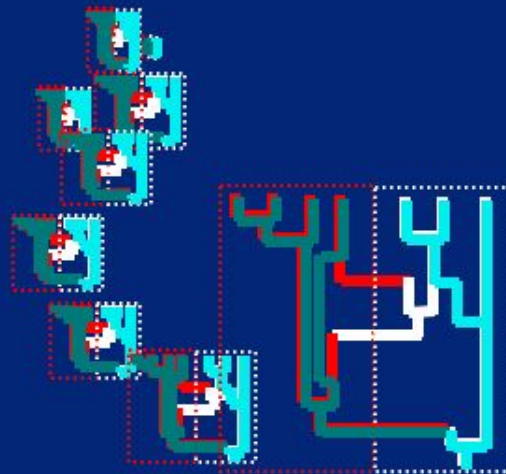


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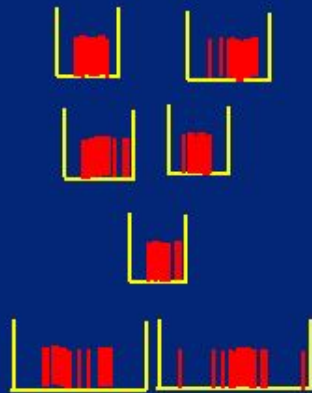


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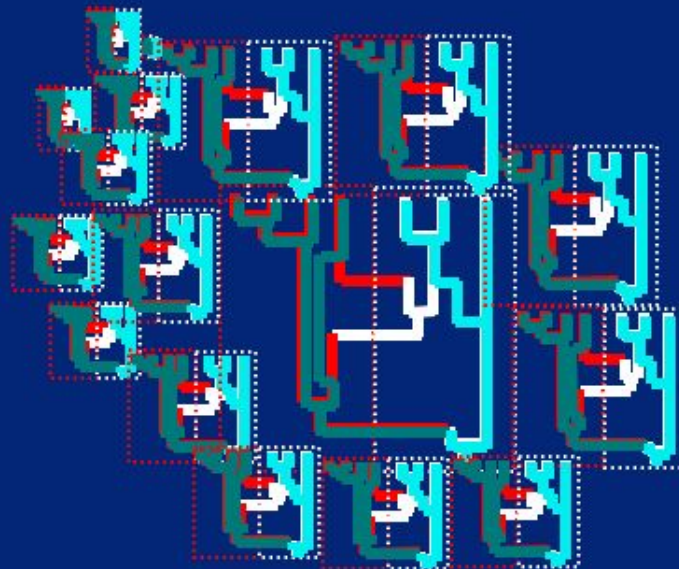


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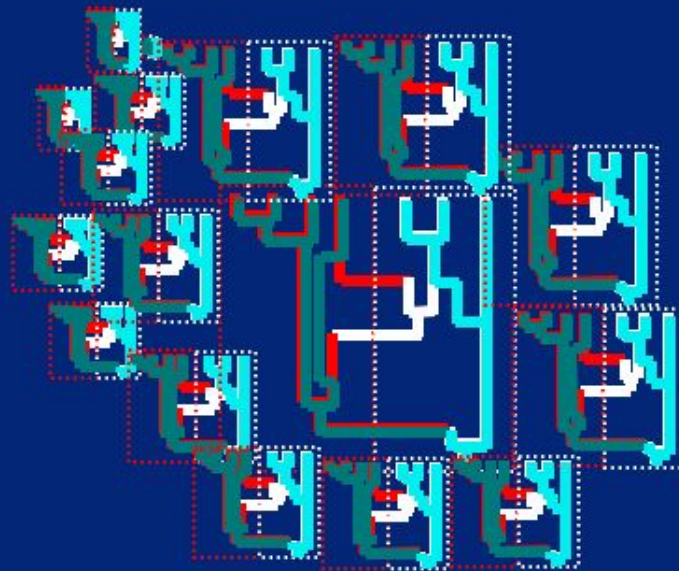
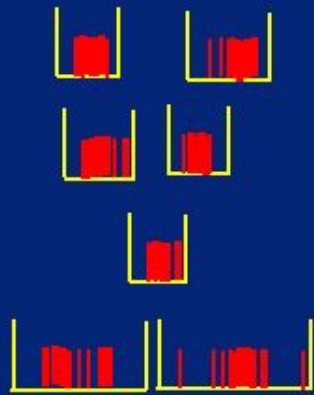
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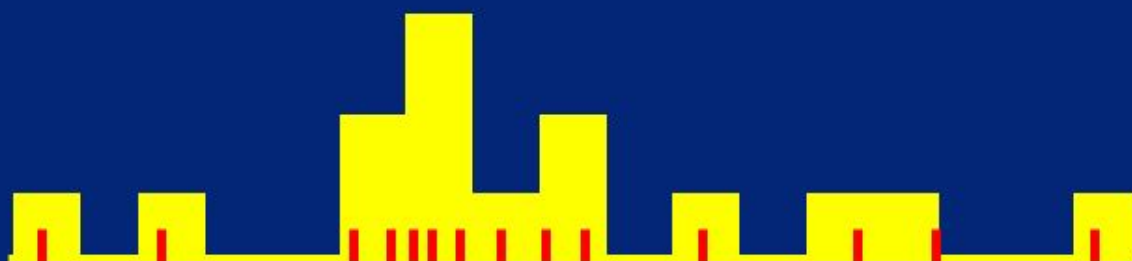


Keep a list of all accepted parameters

Data collection and curve smoothing



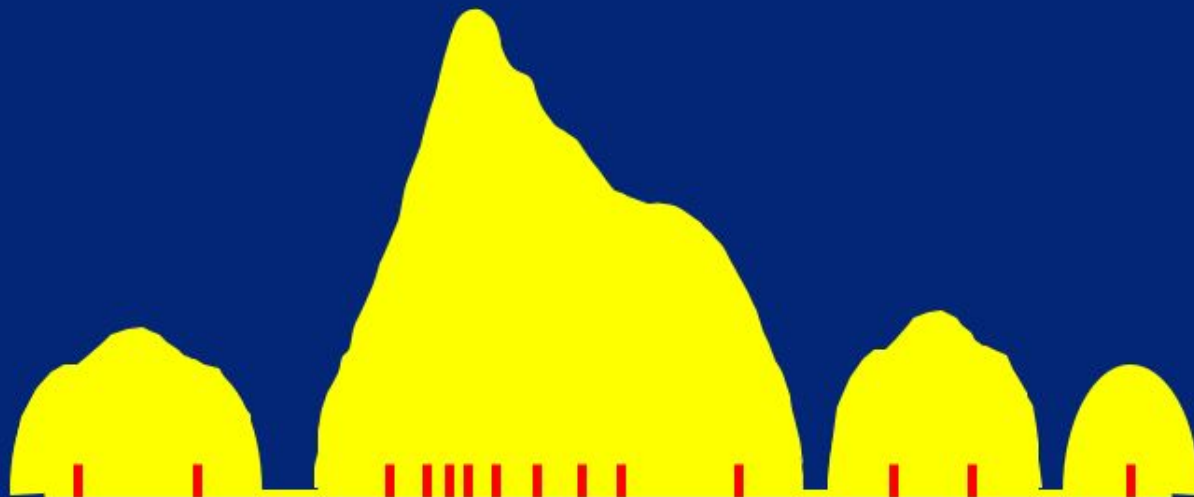
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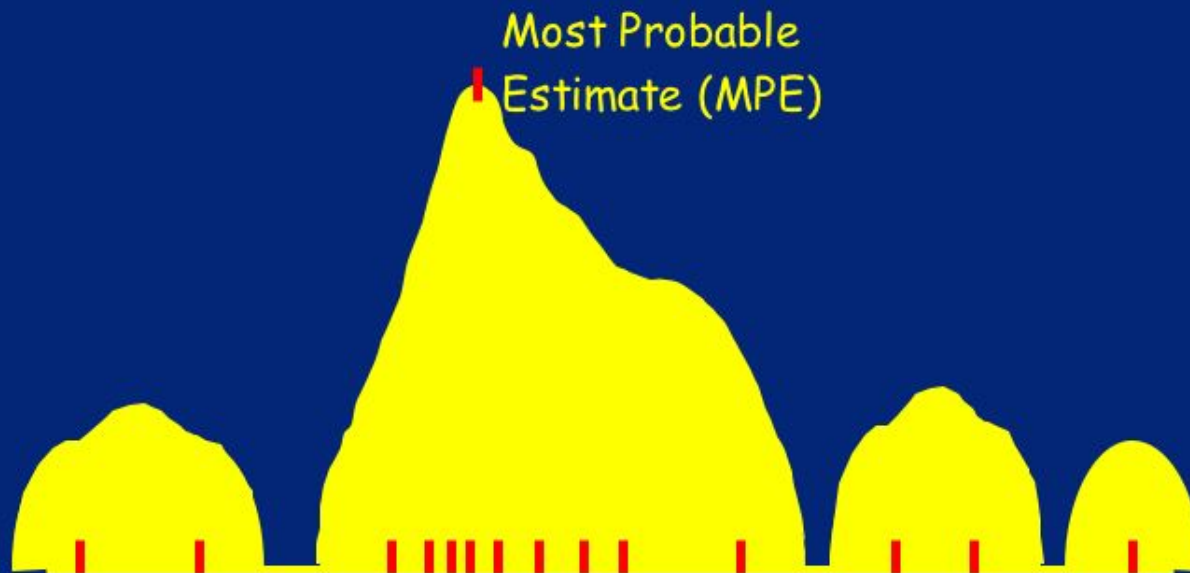
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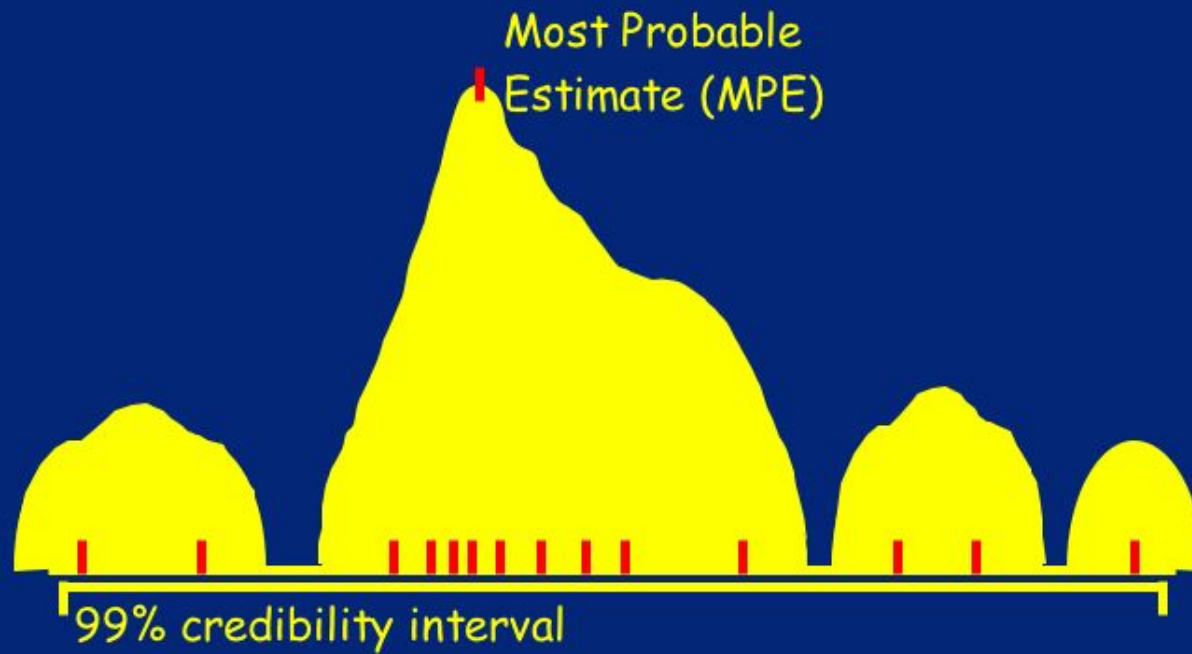
Data collection and curve smoothing



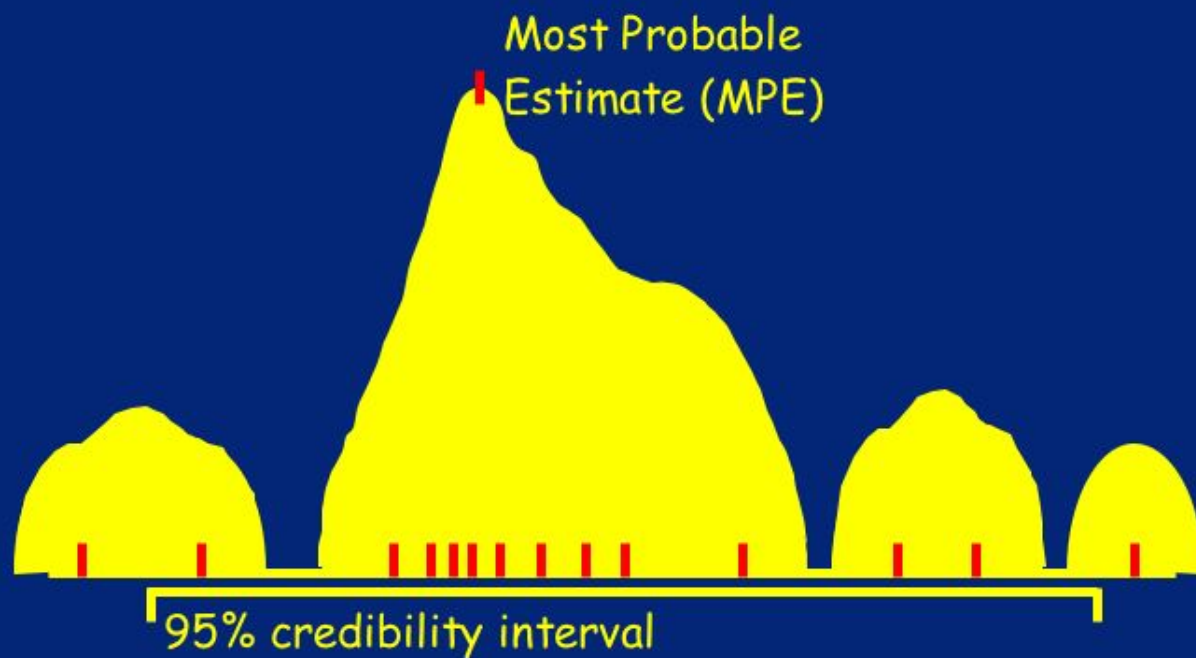
Data collection and curve smoothing



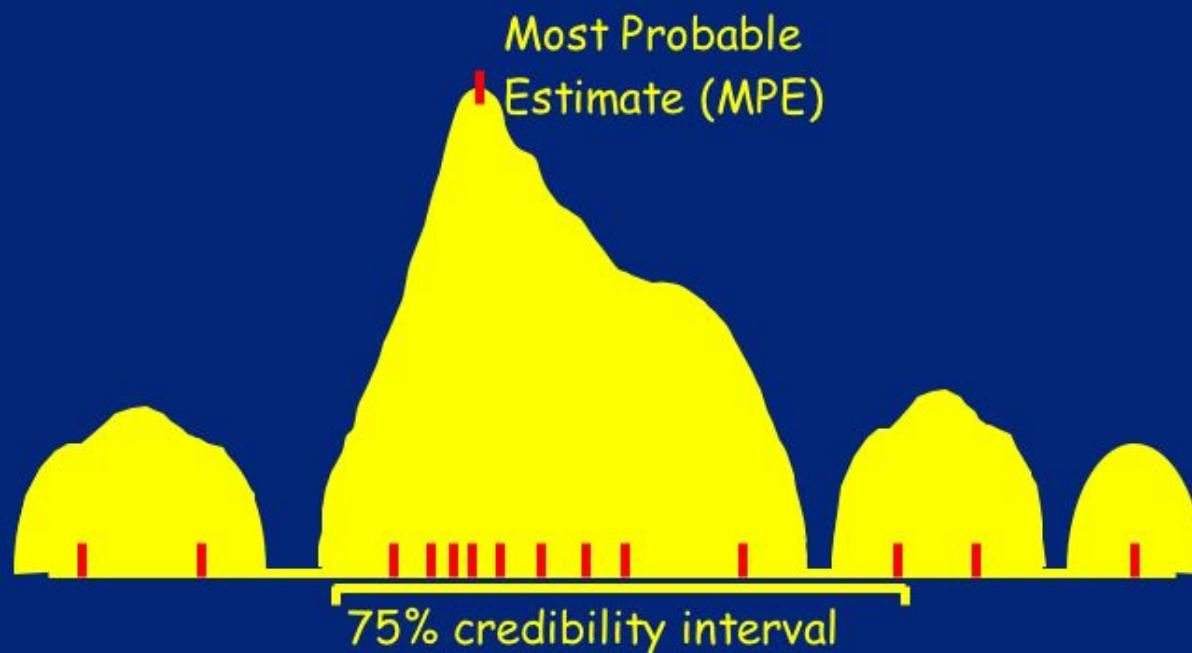
Data collection and curve smoothing



Data collection and curve smoothing



Data collection and curve smoothing



Advantages of Bayesian analysis

- Easier to interpret probabilities than likelihoods
- Smoothing a histogram is quicker than finding maxima of a likelihood curve
- Not dependent on starting driving values
- Parameter values near zero estimated more accurately
- Prior information can be incorporated (in theory)
- Trendy!

Disdvantages of Bayesian analysis

- No information currently available on correlation of parameters
- Dependent on good priors; results can be severely distorted by bad priors

Bottom line

- Kuhner 2006: Bayes and likelihood almost identical
- Beerli 2006: Bayes has edge with sparse data
- My recommendations:
 - Use Bayes if you think a parameter is very close to zero
 - Otherwise, with rich data either method is good
 - With poor data, do you really want to be doing this analysis at all?
 - When using Bayes, be careful of your priors!
- If the genealogy search is inadequate, both methods will fail (and fail in similar ways)

Break

Outline

1. Introduction to coalescent theory

2. Genealogy samplers

3. **Survey of samplers**

(a) **BEAST**

(b) **Genetree**

(c) **IM/IMa**

(d) **Lamarc**

(e) **Migrate-N**

4. Evolutionary forces

5. Practical considerations

BEAST (<http://evolve.zoo.ox.ac.uk/beast/>)

- Drummond and Rambaut
- Estimates:
 - Overall population size x mutation rate
 - Overall growth rate
 - With multiple time points, mutation rate and generation time
 - Detailed skyline plots of growth rate
 - Relaxed molecular clock
- Bayesian analysis
- DNA, RNA, amino acids, codon data, continuous and discrete morphological traits

BEAST

- Strengths:
 - Multiple time point data (ancient DNA, microorganisms)
 - Flexible population growth model
 - Highly flexible mutation model
- Weaknesses:
 - Single population
 - No recombination

IM, IMa2

(<http://lifesci.rutgers.edu/heylib/HeylabSoftware.htm#IM>)

- Nielsen, Hey, Wakeley
- Estimates:
 - Population size x mutation rate
 - Immigration rates
 - Size of ancestral population
 - Time of divergence
 - Daughter population growth rates (IM only)
- Bayesian analysis
- DNA, RNA, microsatellites, HapSTRs
- IM has the most models; IMa2 has more than two populations

IM/IMa2

- Strengths:
 - Correct analysis of young (less than $4N$ generations) populations
 - Distinguishing gene flow from common ancestry
- Weaknesses:
 - Single time point only
 - No recombination
 - Exponential growth only

LAMARC

(<http://evolution.gs.washington.edu/lamarc.html>)

- Kuhner, Beerli, Felsenstein et al.
- Estimates:
 - Population size x mutation rate
 - Immigration rates
 - Growth rates
 - Overall recombination rate
- Likelihood or Bayesian analysis
- DNA, RNA, SNPs, microsats, electrophoretic alleles
- Gene mapping, haplotype inference

LAMARC

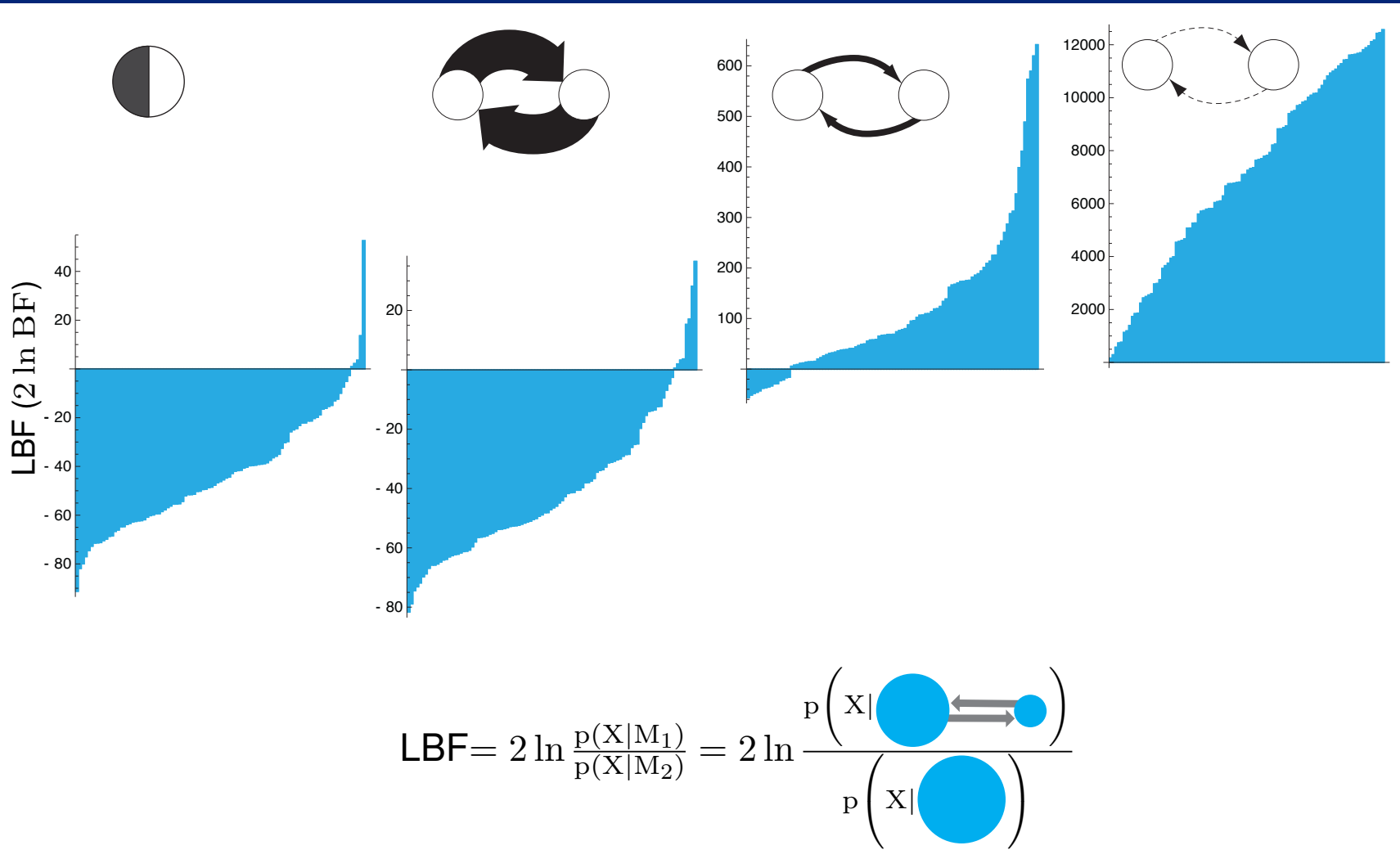
- Strengths:
 - Recombination
 - Data with unknown haplotype phase
 - Combining dissimilar loci
- Weaknesses:
 - Assumes stable population structure (divergence coming soon!)
 - Single time point data only
 - Exponential growth only

MIGRATE-N

(<http://popgen.csit.fsu.edu/Migrate-n.html>)

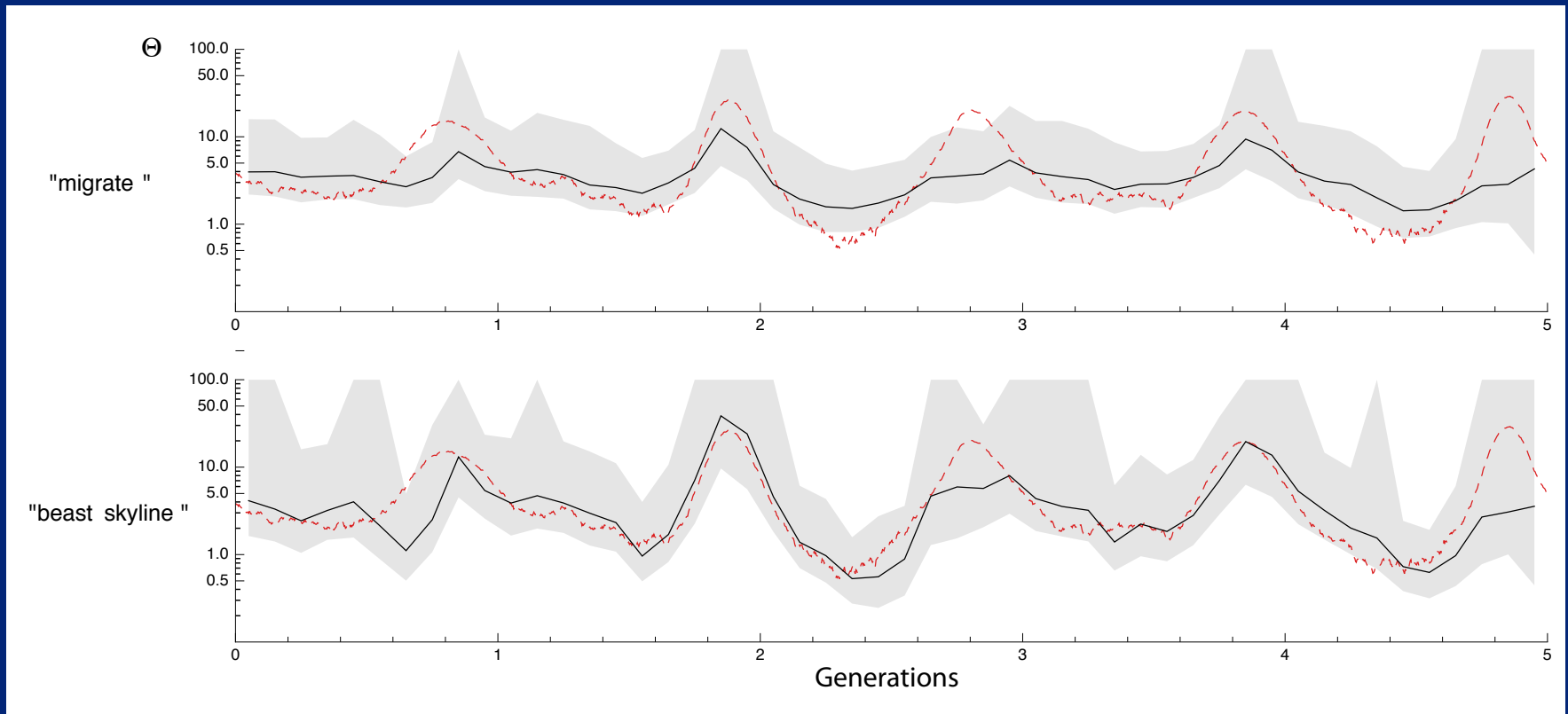
- Beerli
- Estimates:
 - Population size x mutation rate
 - Immigration rates
 - Tests among different migration models
- Likelihood or Bayesian analysis
- DNA, RNA, SNPs, microsats, electrophoretic alleles
- Multiple time points

Bayes factor tests of models



MIGRATE-N

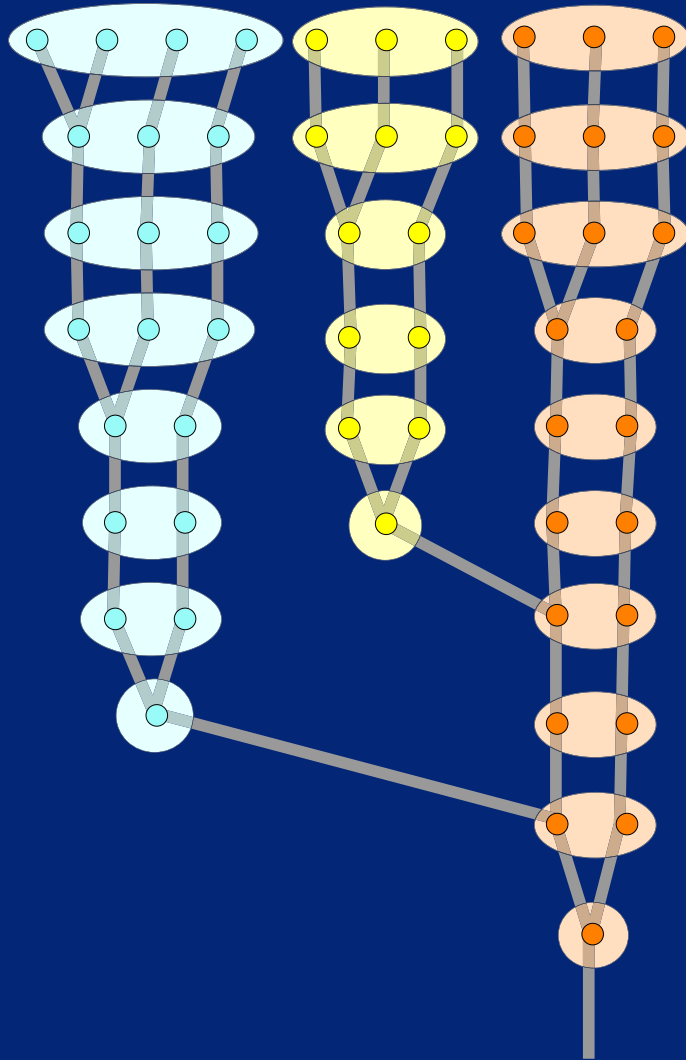
- Strengths:
 - Skyline plots for all parameters
 - Multiple time points
 - Bayes factor tests of different models
- Weaknesses:
 - Assumes stable population structure and size
 - No recombination or growth



Comparison of skyline plots between MIGRATE-N and BEAST for simulated influenza data with multiple time points

Genetree

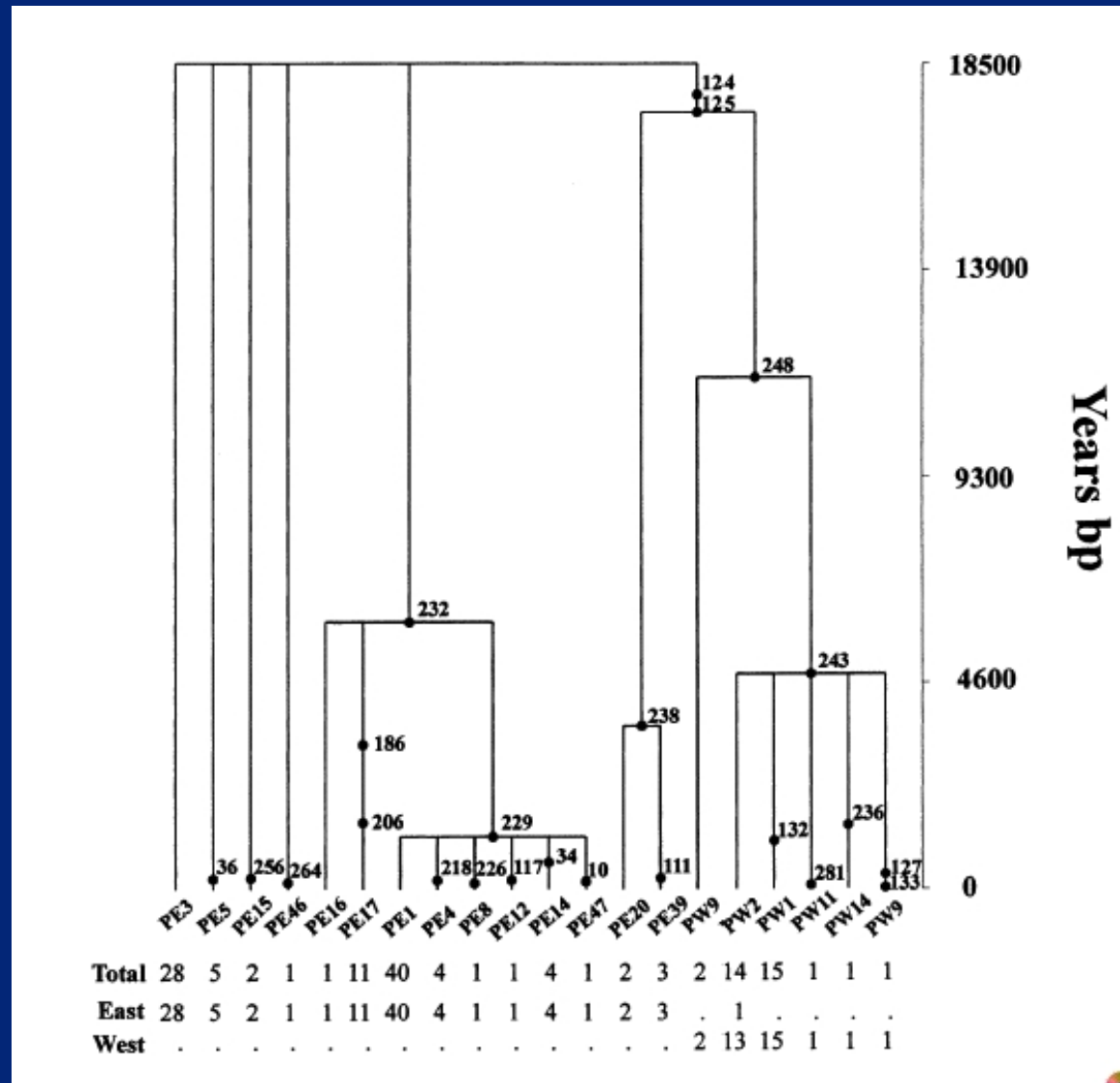
(<http://www.stats.ox.ac.uk/~griff/software.html>)



- Infinite sites model
- Use MCMC to sample a path through the possible histories
- Sample many different possible histories

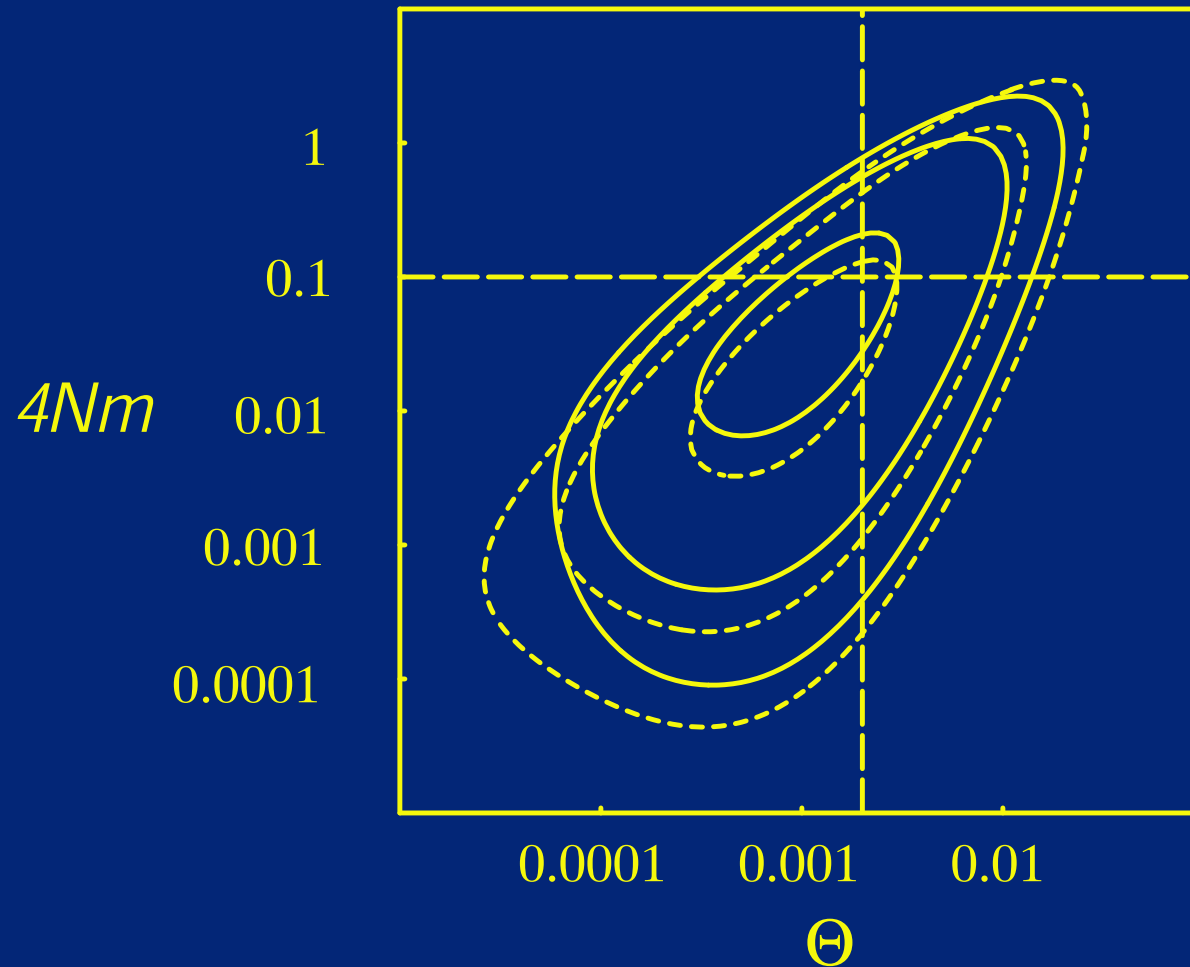
Dating mutations events using *Genetree*

Milot et al. (2000)



Comparison between *Migrate-N* and *Genetree*

(Beerli and Felsenstein 2001)



Genetree

- Strengths:
 - Efficient search
 - Dating of specific mutations
 - Dating of the common ancestor
- Weaknesses:
 - Infinite-sites mutational model only
 - No recombination
 - Exponential growth only
 - Single time point
 - Less developed user interface

Outline

1. Survey of samplers

2. Evolutionary forces

- Genetic drift (Θ)
- Population growth/shrinkage
- Migration
- Recombination
- Population divergence
- Multiple time points
- Haplotype uncertainty
- Disequilibrium mapping

3. Practical considerations

Genetic drift (*Theta*)

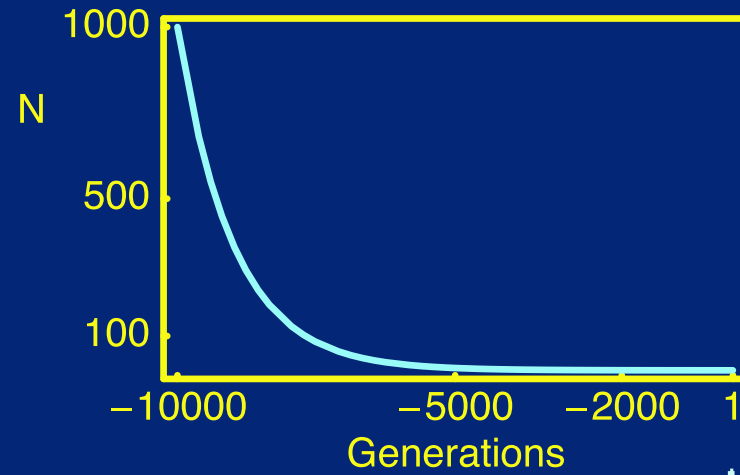
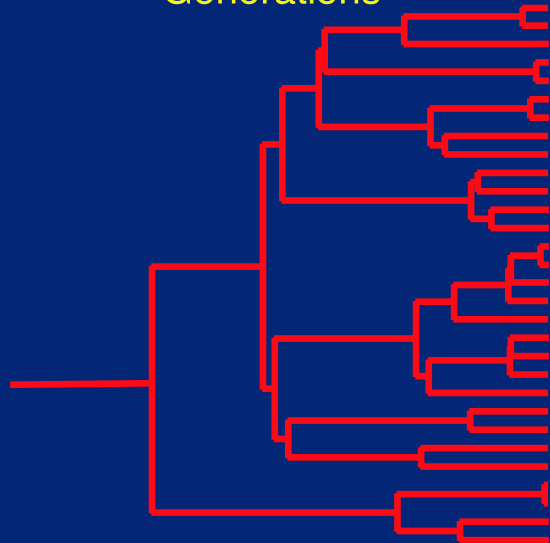
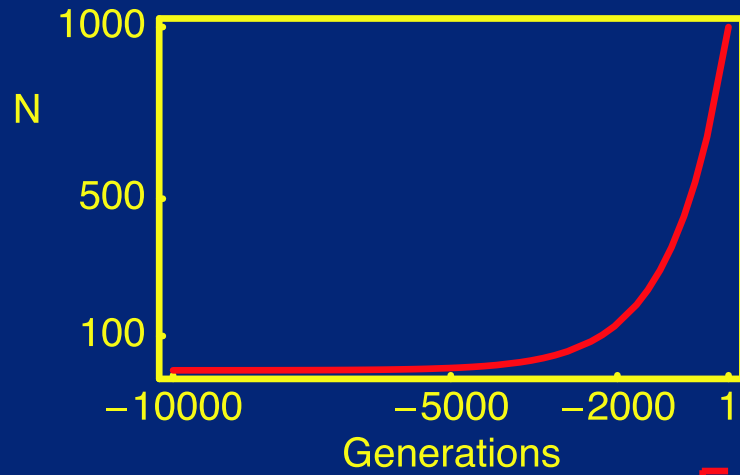
- With one time point, we estimate $\Theta = 4N_e\mu$ in diploids
- The number estimated is $2N_e\mu$ in haploids or $N_e\mu$ in mtDNA
- Two ways to separate N_e and μ :
 - Dated historical data (ancient DNA, etc.)
 - External estimate of mutation rate
- For most organisms, N_e is less than N
- Demographic models can help resolve this

Variable population size

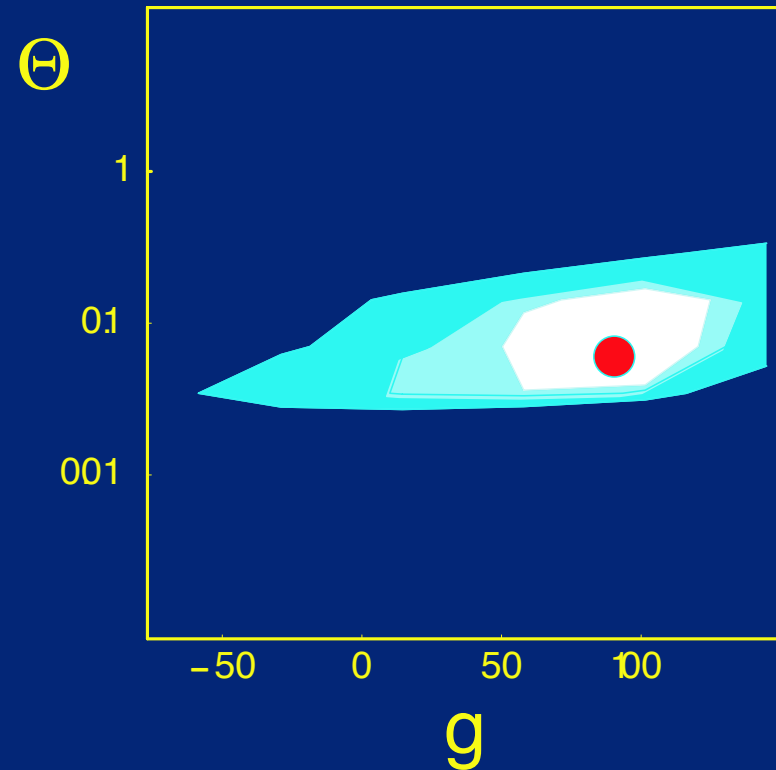
- In a small population lineages coalesce quickly
- In a large population lineages coalesce slowly

This leaves a signature in the data. We can exploit this and estimate the population growth rate g jointly with the current population size Θ .

Exponential population size expansion or shrinkage

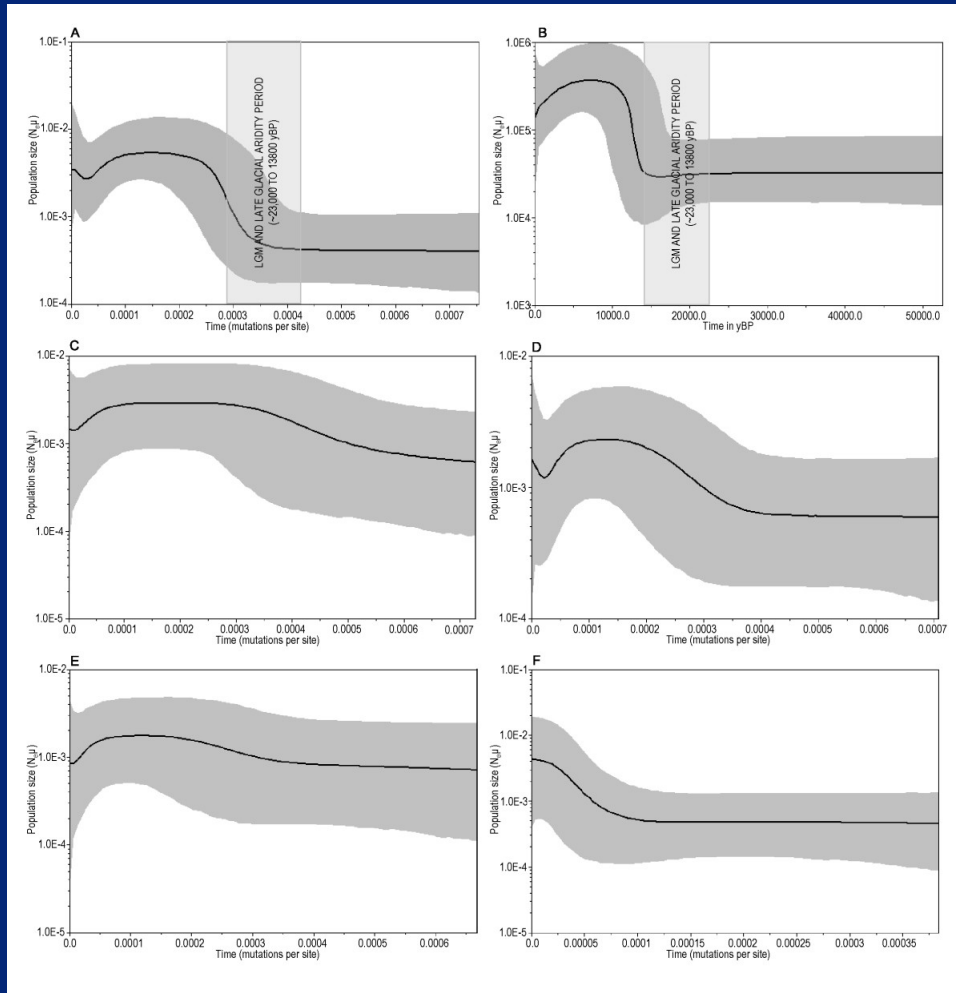


Grow a frog



Mutation Rate	Population sizes	
	-10000 generations	Present
10^{-8}	8,300,000	8,360,000
10^{-7}	780,000	836,000
10^{-6}	40,500	83,600

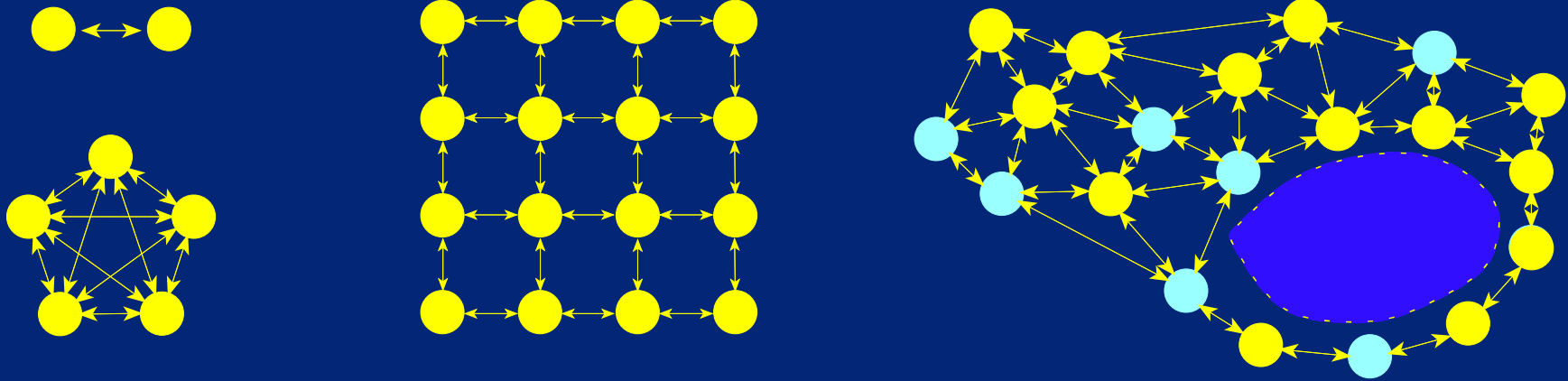
Bayesian skyline plots



Growth estimation software

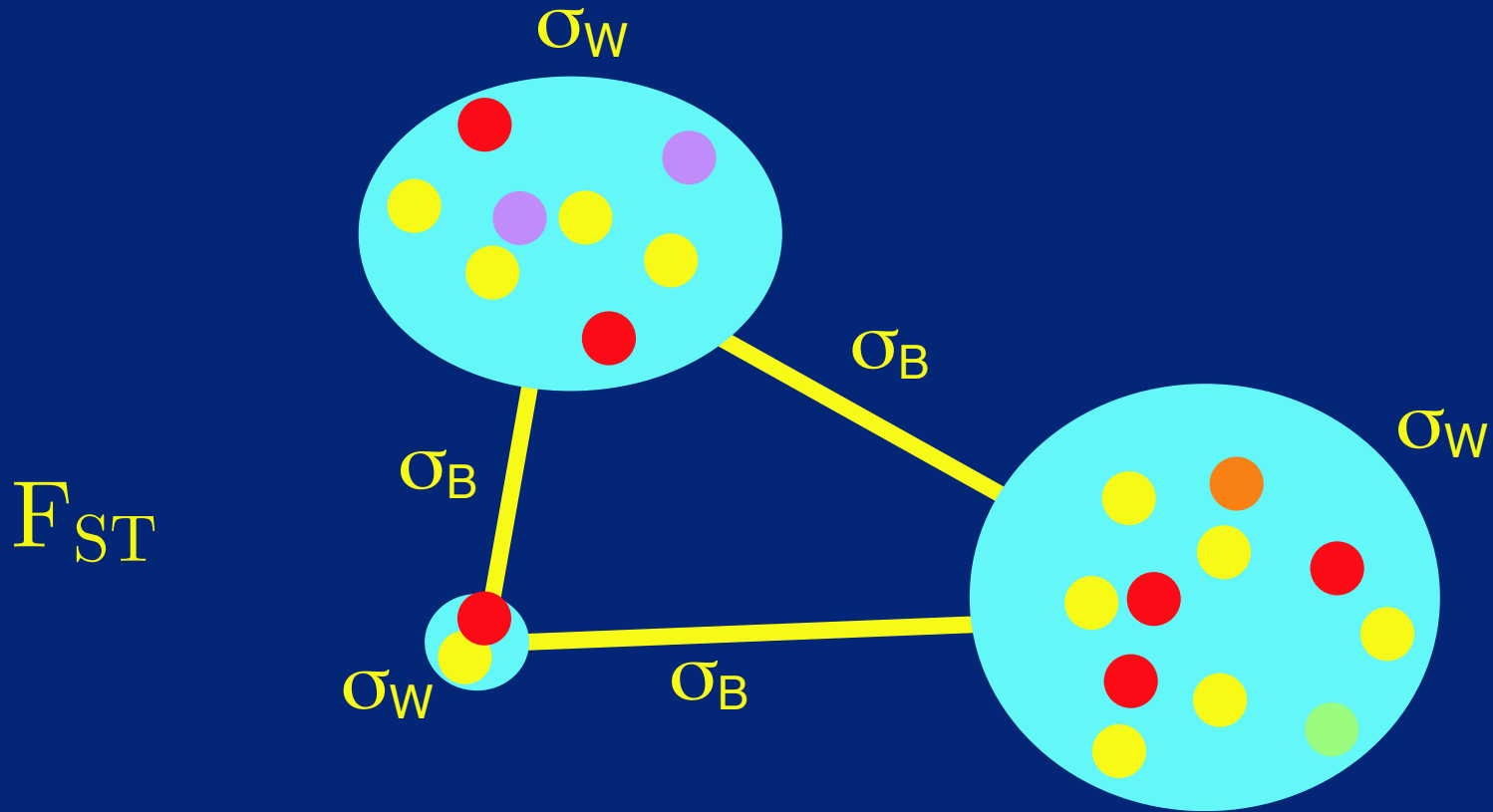
- Currently done with *Lamarc* or *Beast*
- Statistically weaker than estimation of Θ :
 - Biased upwards with one locus/one timepoint
 - Reasonable results with multiple unlinked loci
 - Even better results with multiple timepoints
- *Lamarc* assumes exponential growth/shrinkage
- *Beast* has a generalized model

Gene flow

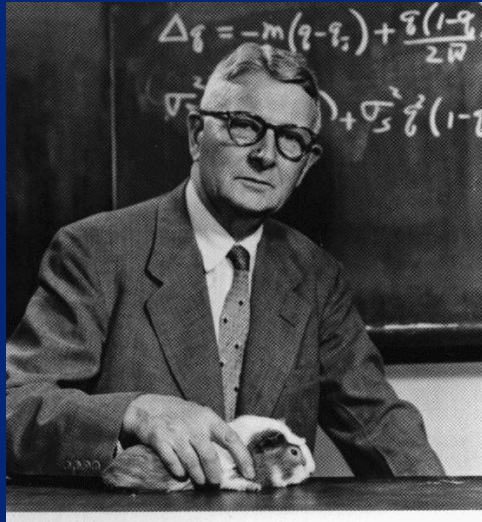


$$p(G|\Theta, \mathbf{M}) = \prod_{u_j} \left(\prod_i^{\text{pop.}} g(\Theta_i, \mathbf{M}_{.i}) \right) \begin{cases} \frac{2}{\Theta} & \text{if event is a coalescence,} \\ M_{ji} & \text{if event is a migration from } j \text{ to } i. \end{cases}$$

Gene flow: What researchers used (and still use)



What researchers used (and still use)



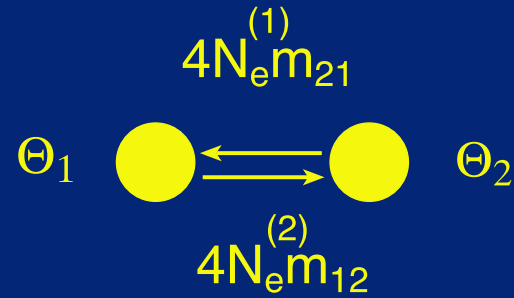
Sewall Wright showed that

$$F_{ST} = \frac{1}{1 + 4Nm}$$

and that it assumes

- migration into all subpopulation is the same
- population size of each island is the same

Simulated data and Wright's formula



True values	Estimated values
0.01 $\xleftrightarrow{1.}$ 0.01 $\xleftarrow{1.}$	1.14 ± 0.77
0.01 $\xleftrightarrow{10.}$ 0.01 $\xleftarrow{1.}$	7.80 ± 22.20
0.05 $\xleftrightarrow{10.}$ 0.005 $\xleftarrow{1.}$	11.46 ± 18.54

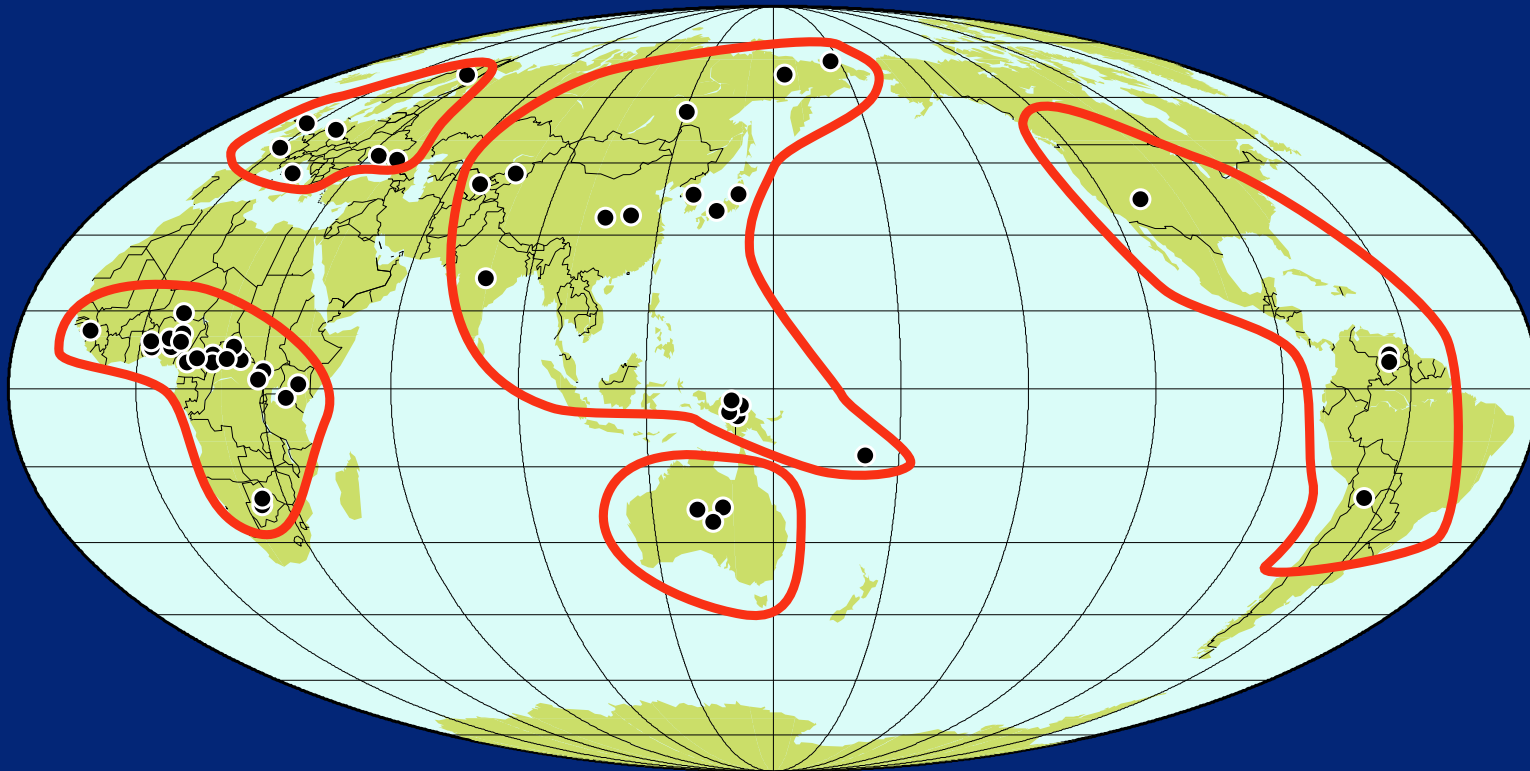
Maximum Likelihood method to estimate gene flow parameters

(Beerli and Felsenstein 1999)

100 two-locus datasets with 25 sampled individuals for each of 2 populations and 500 base pairs (bp) per locus.

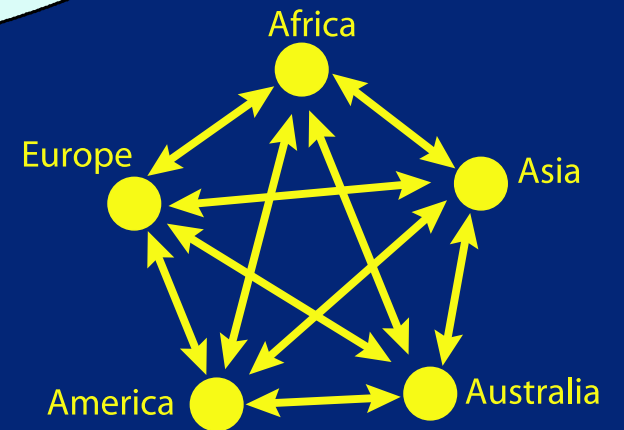
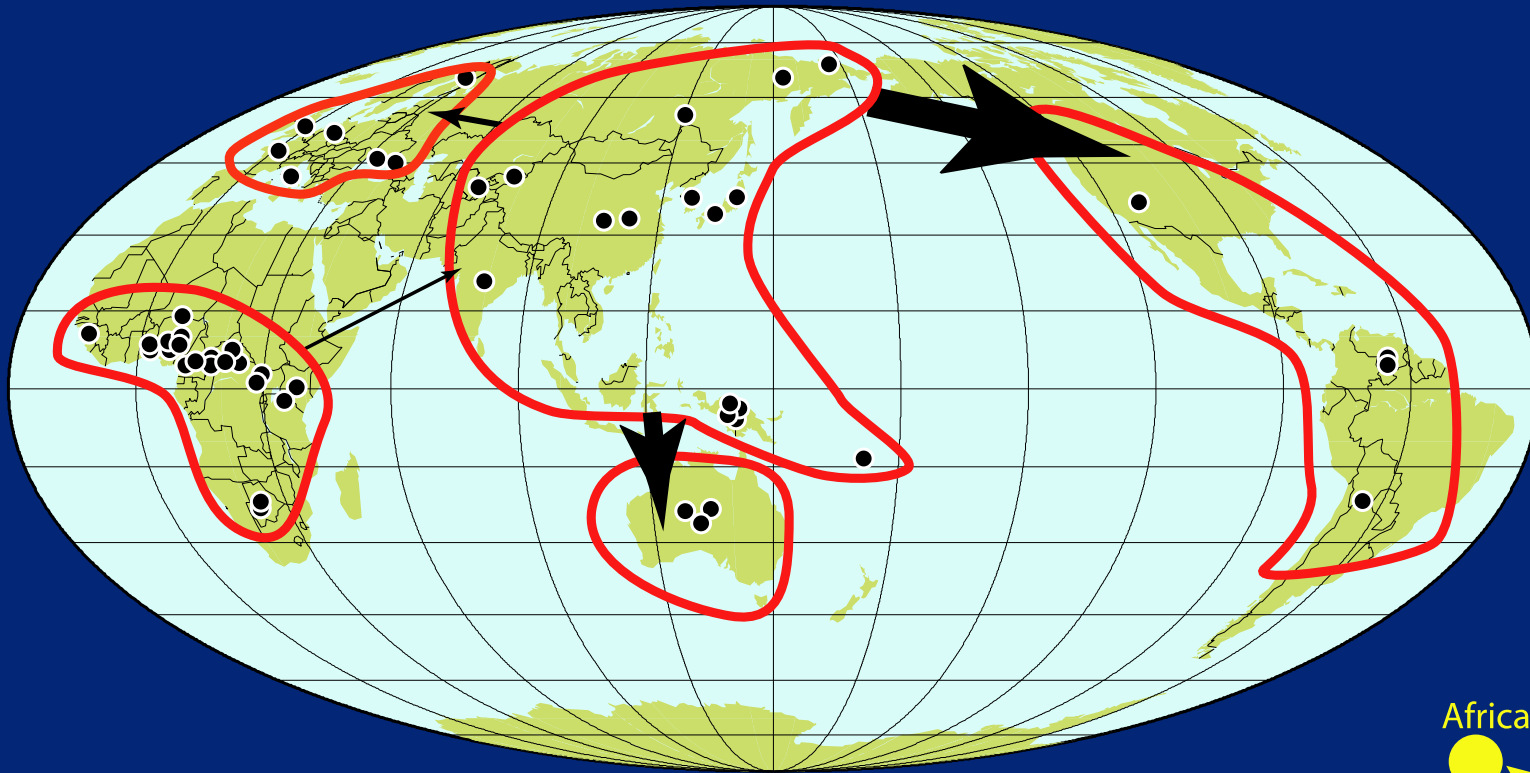
	Population 1		Population 2	
	Θ	$4N_e^{(1)}m_1$	Θ	$4N_e^{(2)}m_2$
Truth	0.0500	10.00	0.0050	1.00
Mean	0.0476	8.35	0.0048	1.21
Std. dev.	0.0052	1.09	0.0005	0.15

Complete mtDNA from 5 human “populations”

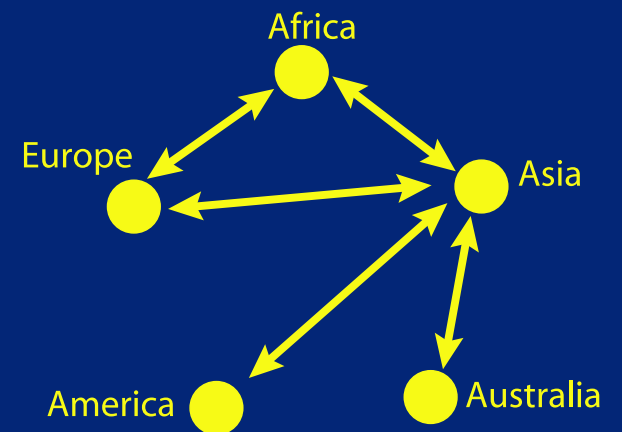
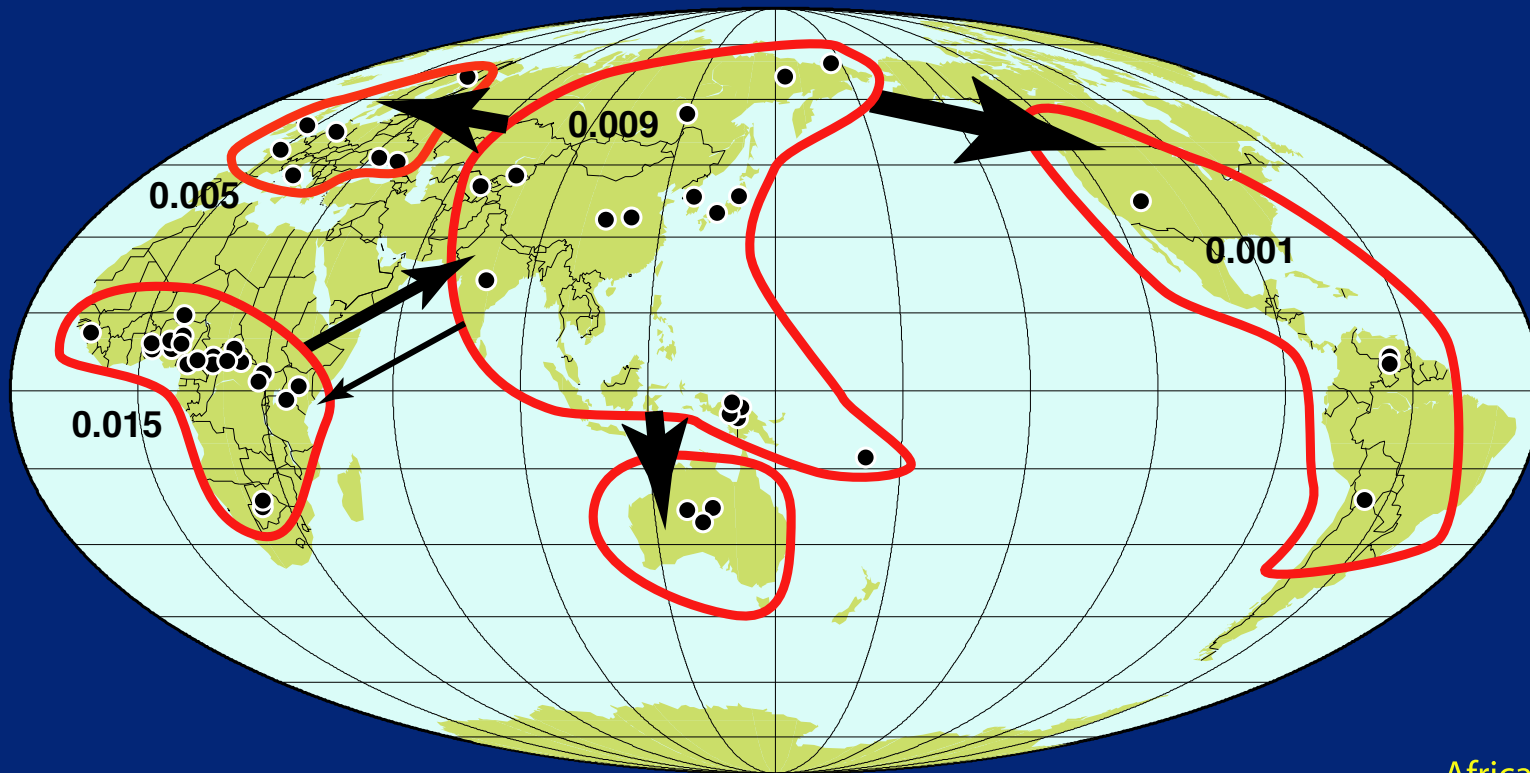


A total of 53 complete mtDNA sequences (~ 16 kb):
Africa: 22, Asia: 17, Australia: 3, America: 4, Europe: 7.
Assumed mutation model: F84+ Γ

Full model: 5 population sizes + 20 migration rates



Restricted model: only migration into neighbors allowed



Coalescent migration estimation

- Done by *Lamarc*, *Migrate-N*, *IM/IMa* estimating:
 - Θ per subpopulation
 - Immigration from each subpopulation into each of the others
- *Lamarc* and *Migrate-N* assume stable population structure
- *IM/IMa* assume divergence of two or more populations from a common ancestor

Recombination rate estimation

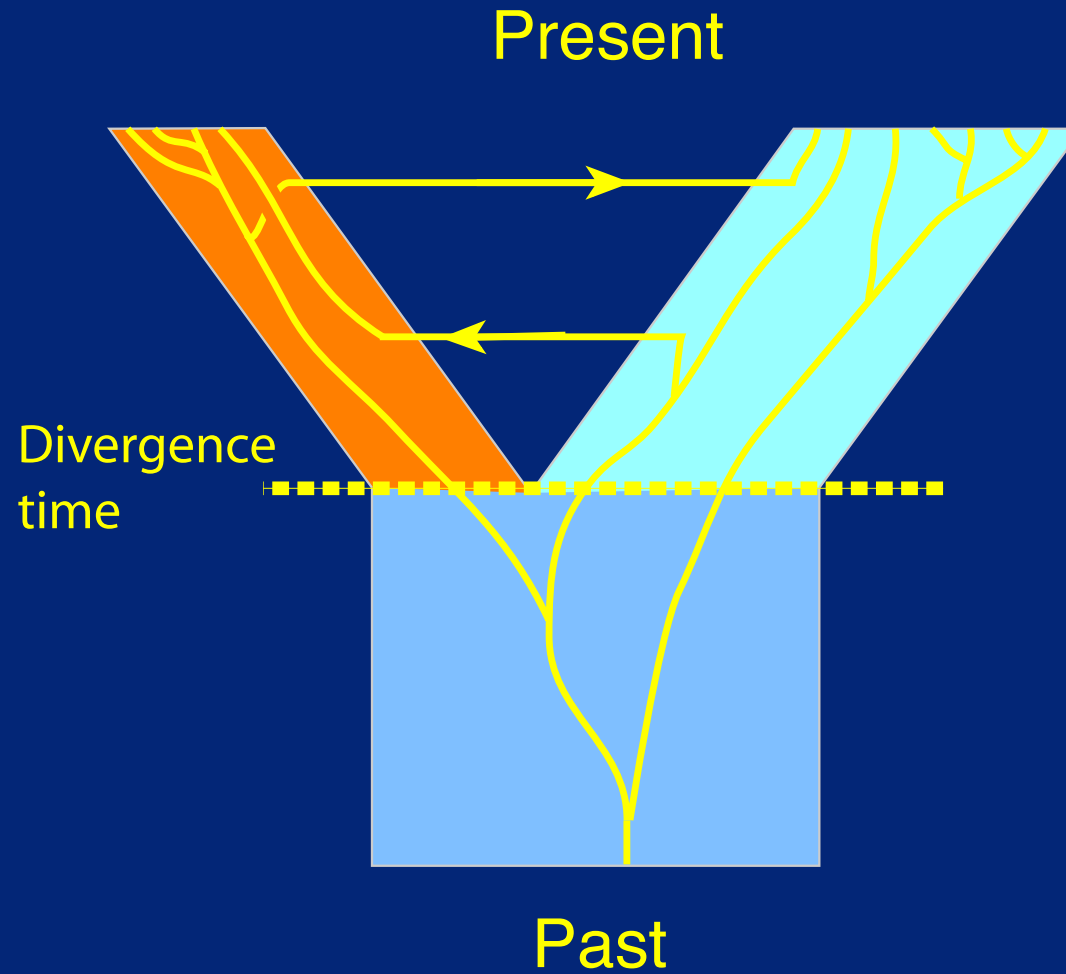


Coalescent recombination estimators

- Previously done with *Recombine*
- Currently done with *Lamarc*
- Assumptions:
 - No gene conversion
 - Equal recombination rate at every site
- Allows correct use of data with recombination to estimate other parameters
- Use of recombining data in a non-recombination-aware algorithm leads to bias

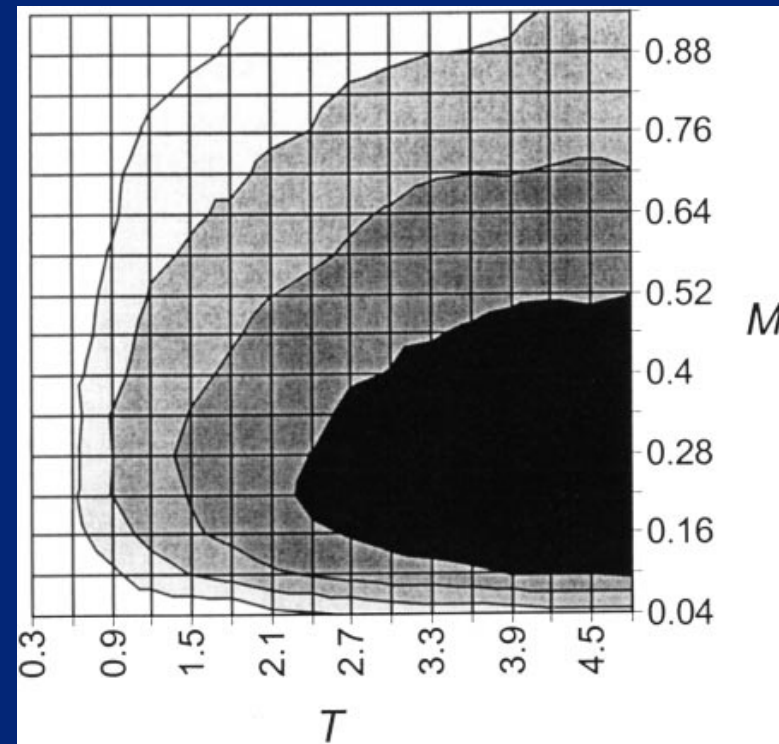
Estimation of divergence time

Wakeley and Nielsen (2001)



Estimation of divergence time

Wakeley and Nielsen (2001) Figure 7. The joint integrated likelihood surface for T and M estimated from the data by Orti et al. (1994). Darker values indicate higher likelihood.



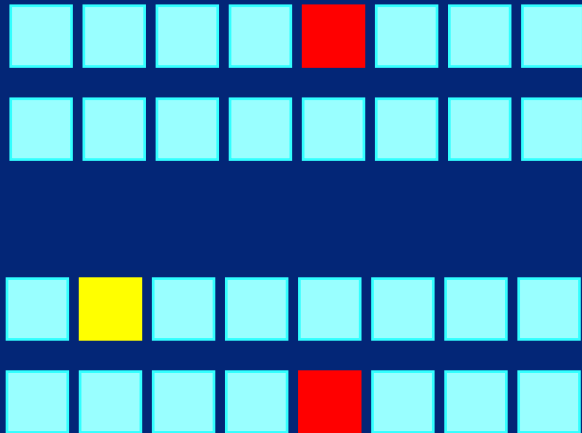
Coalescent divergence estimators

- Done with *IM/IMa*
- Up to 10 populations
- Co-estimates divergence time, migration rates and populations sizes
- Not all data sets can separate migration from divergence
- Multiple loci are helpful

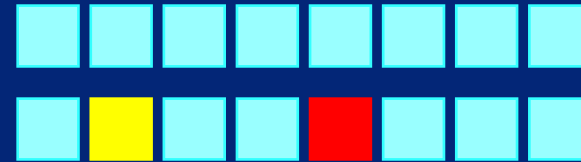
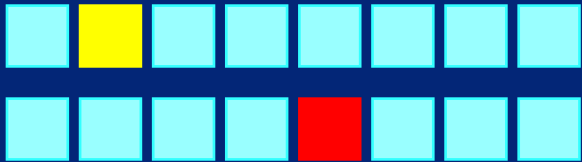
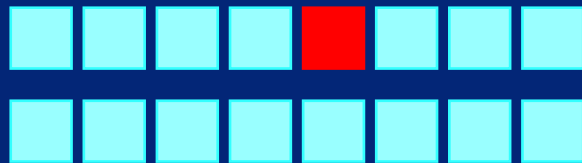
Multiple time points

- Ancient DNA or historical samples of fast-evolving organisms
- Done with *Beast* or *Migrate-N*
- Points must be:
 - Dated
 - Far enough apart for measurable evolution
- Advantages:
 - Separation of Θ into N_e and μ
 - Much better resolution of growth rates

Haplotype uncertainty



Haplotypes



Either haplotypes must be resolved or the program must integrate over all possible haplotype assignments.

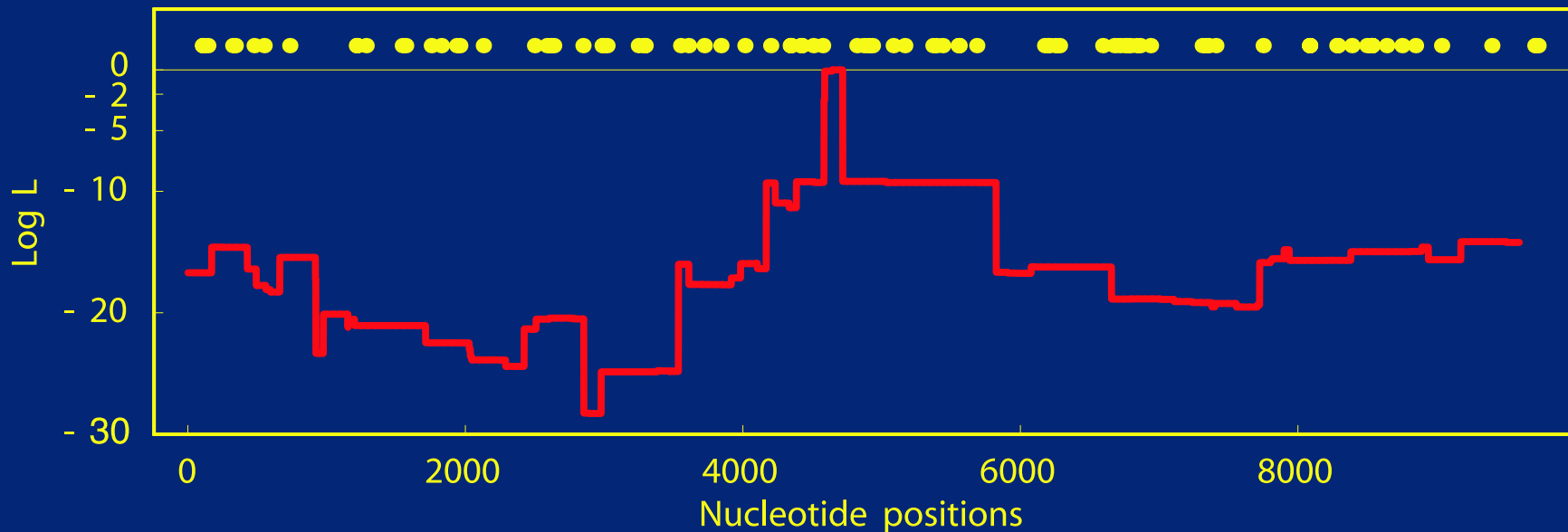
Currently only *Lamarc* can do the latter.

MCMC versus best-fit haplotypes

- Advantages of MCMC:
 - Avoids bias of "too good" best fit
 - Incorporates error of haplotypes into error estimates
- Advantages of best-fit haplotyping:
 - Much faster
 - Avoids MCMC search failure issues
 - Can use external evidence about best haplotypes

Linkage disequilibrium mapping

With a disease mutation model we can use the recombination estimator to post-analyze the sampled genealogies that were used to estimate r and find the location of the disease mutation on the DNA.



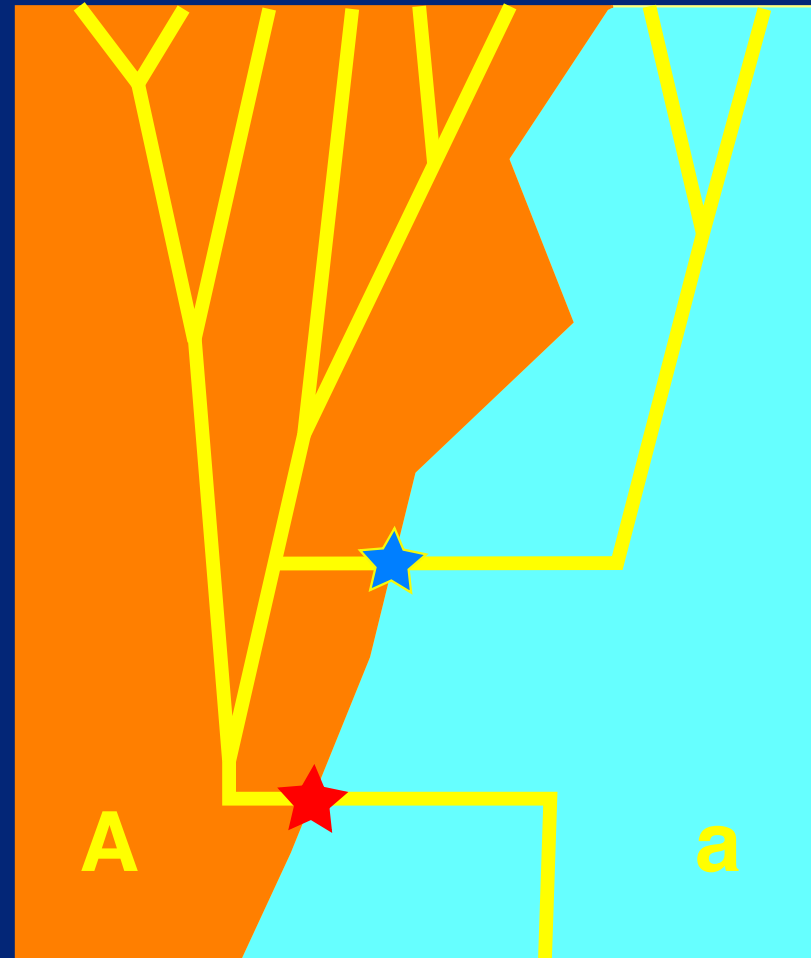
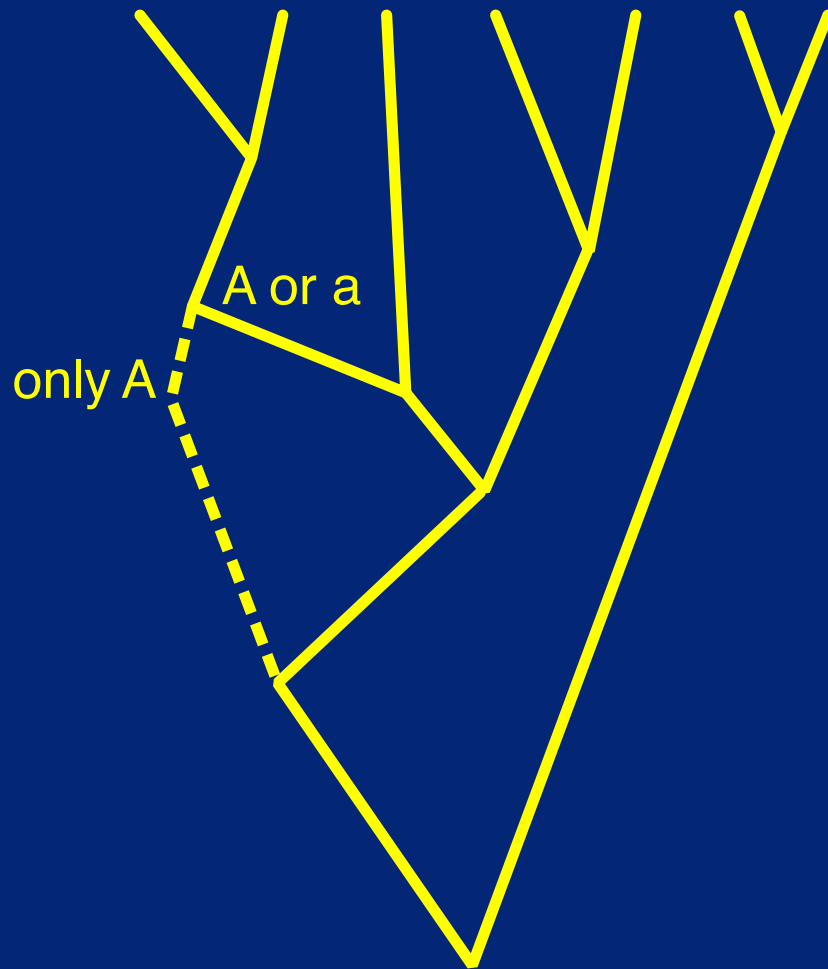
Linkage disequilibrium mapping

Lamarc can perform this type of mapping.

- Takes phenotype data with penetrance model
- Handles haplotype uncertainty
- Currently limited in the size of case it can handle
- We hope to relax this limitation soon

Selection coefficient estimation

Krone and Neuhauser (1999), Felsenstein (unpubl)



Outline

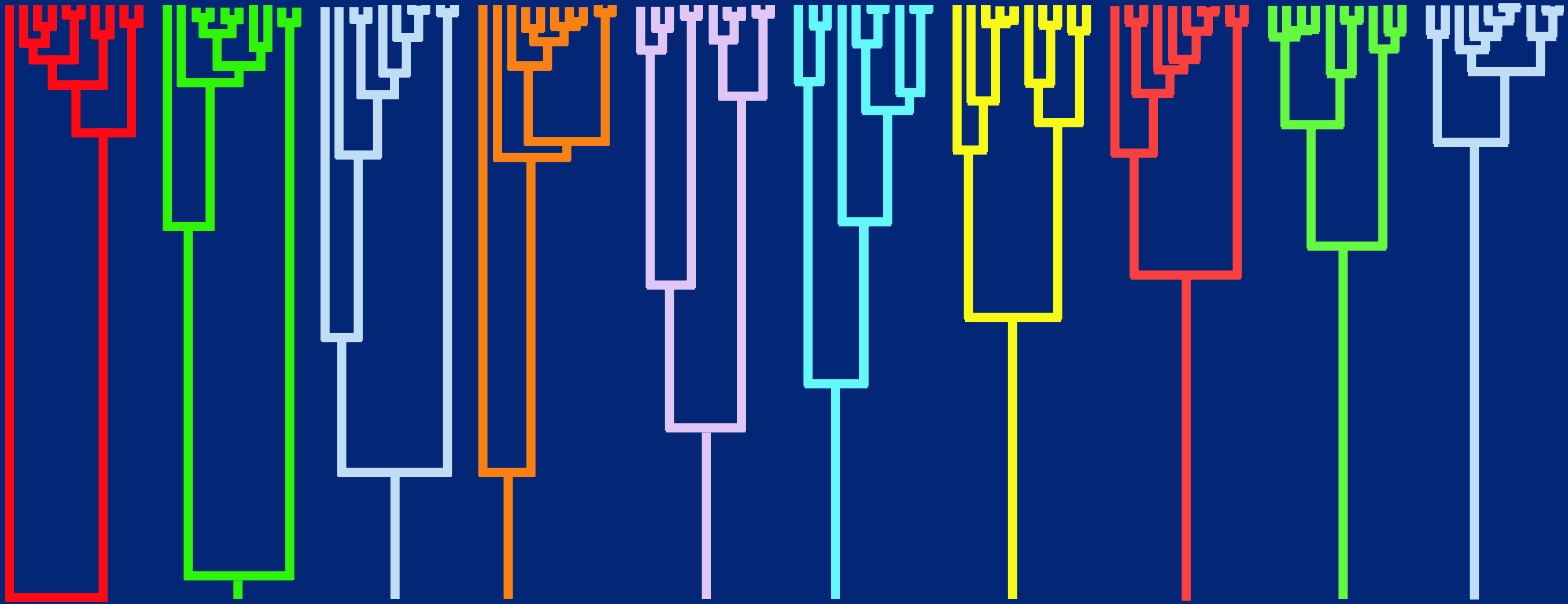
- Introduction to coalescent theory
- Genealogy samplers
- Survey of samplers
- Evolutionary forces
- **Practical considerations**

Information content of the coalescent

What can best give us more information?

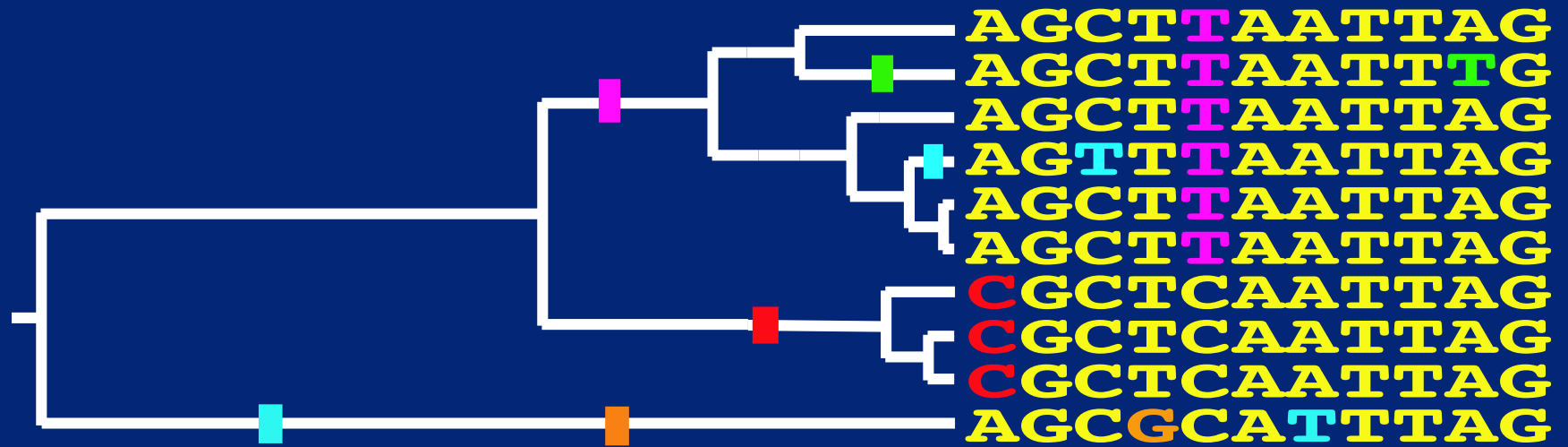
- More individuals?
- More base pairs?
- More loci?

Variability of the coalescent

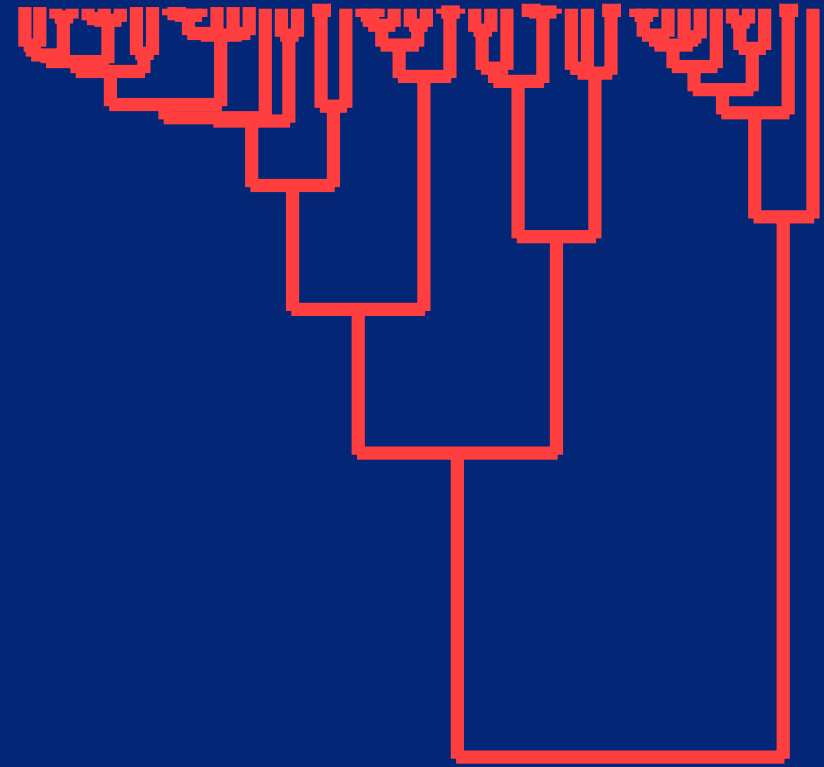
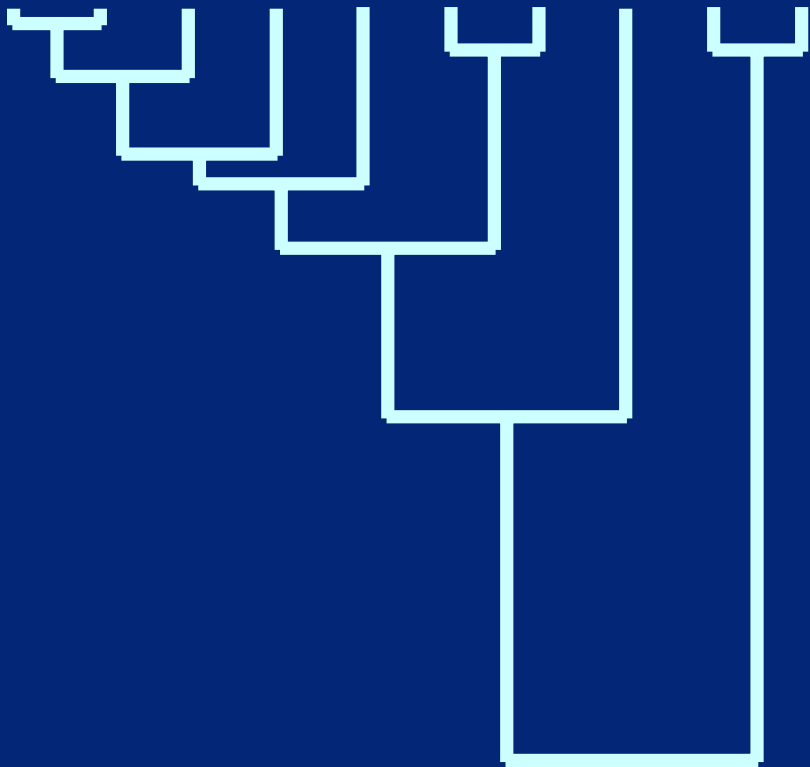


10 coalescent trees generated with the same population size, $N = 10,000$

Variability of mutations



Does adding more individuals help?



The bottom line

- The information content of a single locus is limited
- Additional sequence length or individuals are only mildly helpful
- Multiple loci allow the best estimates
- If recombination is present, long sequences can partially substitute for multiple loci
- Multiple time points can also help, if significant evolution happens between them

Two publications supporting this conclusion

- Felsenstein, J (2005) Accuracy of coalescent likelihood estimates: Do we need more sites, more sequences, or more loci? *MBE* 23: 691-700.
- Pluzhnikov A, Donnelly P (1996) Optimal sequencing strategies for surveying molecular genetic diversity. *Genetics* 144: 1247-1262.

Practical advice

- The major practical problem: how long to run the program?
- Additionally: how many chains, how many steps per chain?



The problem of defaults

- Length of run varies hugely with data and model
- There are no good defaults
- Programs normally ship with defaults which let you see results quickly
- *These are not suitable for publication runs!*

Parameter estimates are still changing

If your estimate of a parameter looks like this:

Chain	Θ
1	0.0035
2	0.0047
3	0.0088
4	0.0105
5	0.0121

you have not run the program long enough. It's probably best to increase the number of steps in each chain.

Parameter estimates are still changing

If your estimate of a parameter looks like this:

Chain	Θ
1	0.0035
2	0.0047
3	0.0088
4	0.0105
5	0.0121

you have not run the program long enough. It's probably best to increase the number of steps in each chain.

You would prefer to see this:

Chain	Θ
1	0.0056
2	0.0098
3	0.0110
4	0.0107
5	0.0109

Trees aren't being accepted

If almost all trees are being rejected, the sampler obviously cannot move well.

- This might be due to a bad starting value
- More likely it shows a need for heating

Parameter values leap around

If your estimate of a parameter looks like this:

Chain	r
1	0.0005
2	0.0047
3	0.0001
4	0.1105
5	0.0021

- Your chains may be too short. (Each visits only one of multiple peaks.)
- Your data may have no power.

Program takes forever to run

- You may be asking too much
- If estimating migration, try restricting your migration model
- Disable or fix at constant values parameters you aren't interested in
- Try randomly removing some individuals
 - More than 20 individuals per population doesn't help much
 - Don't systematically remove similar sequences!
- Borrow a faster computer with lots of memory

Error bars too wide

- Particularly common with growth and recombination estimates
- Usually not an error in your run
- Badly performing genealogy samplers get estimates that are TOO NARROW
- If yours are too wide:
 - Limit the number of parameters being inferred
 - Add unlinked loci
 - Add time points
 - Add sequence length, if recombination present
- Always publish error bars; point estimates have no meaning without them

Validating genealogy samplers

Two useful tools:

- TRACER (Drummond and Rambaut)
 - ESS statistic
 - Traces of parameters throughout the run
 - Histograms of parameter values
- AWTY (Swofford)
 - Traces of clade probabilities throughout the run

Review paper

Kuhner MK (2008) Coalescent genealogy samplers: windows into population history. TREE 24:86-93.

Thanks to

Joe Felsenstein

Peter Beerli

Jon Yamato

Lucrezia Bieler

Elizabeth Thompson

Eric Rynes

Lucian Smith

Elizabeth Walkup

What was the long-term population size of gray whales?



Alter, Rynes and Palumbi (2007) DNA evidence for historic population size and past ecosystem impacts of gray whales. PNAS 104: 15162-15167.

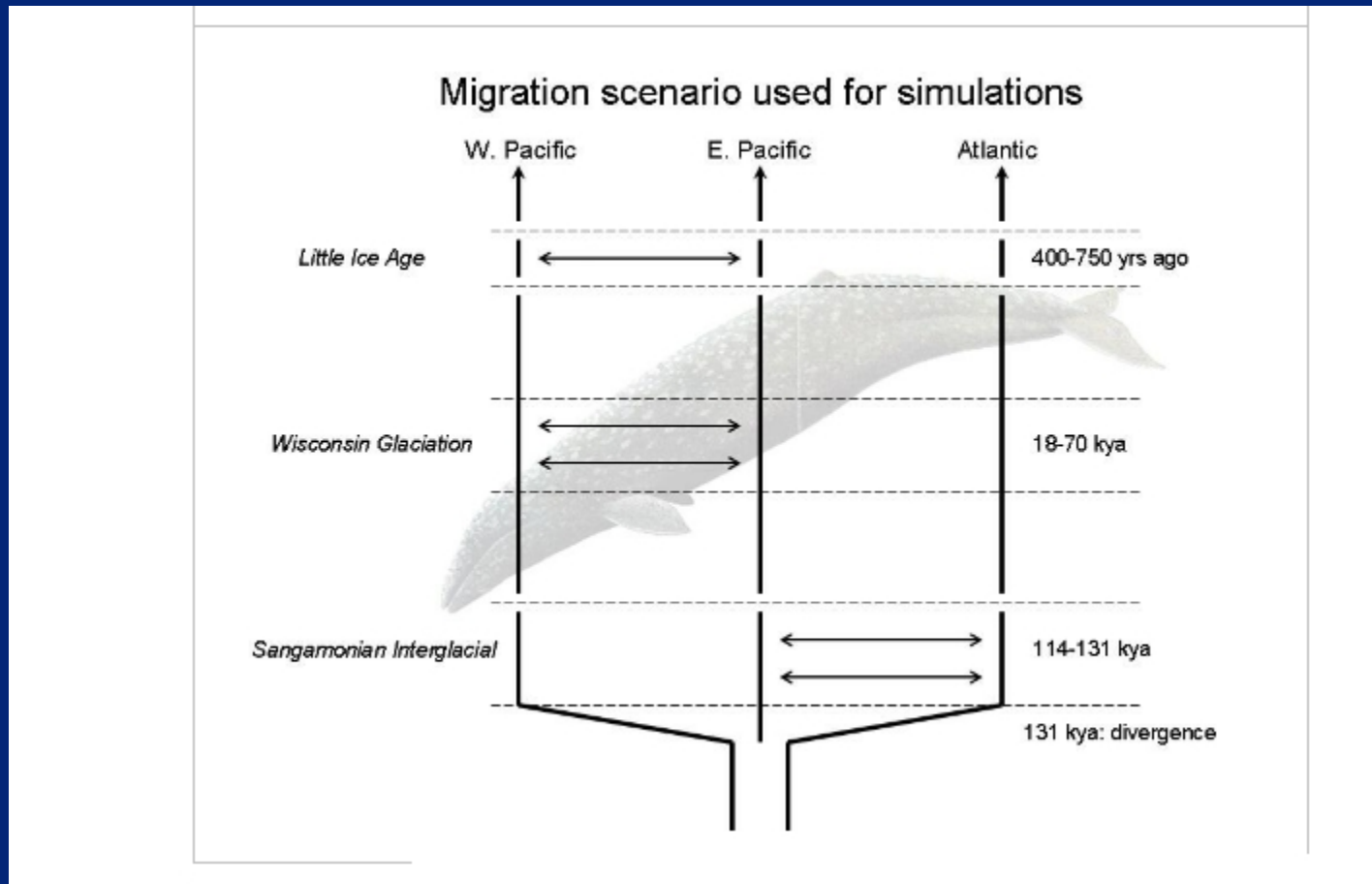
What was the long-term population size of gray whales?

- How many gray whales pre-whaling?
- Whaling ship records not conclusive
- Recent slowing of the observed growth rate may suggest recovery
- Molecular data an alternative source of information

What was the long-term population size of gray whales?

- 10 loci:
 - 7 autosomal
 - 2 X-linked
 - 1 mtDNA
- Complex mutational model with rate variation among loci
- Complex population model with subdivision and copy number
- Complex demographic model relating N_{census} to N_e

What was the long-term population size of gray whales?



What was the long-term population size of gray whales?

	Locus	n	Estimated N
Aut	ACTA	72	162,625
	BTN	72	76,369
	CP	76	77,319
	ESO	72	272,320
	FGG	72	180,730
	LACTAL	72	44,410
	WT1	80	51,972
X	G6PD	30	2,769
	PLP	52	92,655
mtDNA	Cytb	42	107,778
	All data		96,400 (78,500-117,700)
	Current census		18,000-29,000
	Previous models		19,480-35,430

What was the long-term population size of gray whales?

- Important conservation implications
- Effect on ecosystem significant:
 - Resuspension of up to 700 million cubic meters sediment
 - (12 Yukon Rivers worth)
 - Food for 1 million sea birds
- If accepted, result suggests halving gray whale kill rate
- Broadly similar results for minke, humpback, and fin whales