## 2071 Lab 5: Norms, errors and whatnot

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## Introduction

- Two sessions
- Vector and matrix norms, compatibility
- False "proof": spectral radius is not always compatible

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- Residual and solution error
- Relative errors
- Special tridiag matrix (dif2)
- Determinants

## Exercises

- 1.  $L^1$ ,  $L^2$ ,  $L^\infty$  vector norms
- 2. Compatibility between vector and matrix norms
- 3. Example:  $L^2$  is not compatible with spectral radius
- 4. See what happens to iterates when using this matrix
- 5. L<sup>2</sup>-norm is much slower than Frobenius norm
- 6. 4 cases of comparisions between residual and solution norms

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- You can "see" the exact solutions.
- 7. Use relative norms for errors!
- 8. Facts about tridiagonal.m (dif2) matrix
- 9. Determinant for tridiagonal matrix
- 10. (extra) Determinant function for arbitrary matrices.
  - Recursion is inefficient in this case